

Performance Measurement in Blind Audio Source Separation

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Abstract—In this paper, we discuss the evaluation of blind audio source separation (BASS) algorithms. Depending on the exact application, different distortions can be allowed between an estimated source and the wanted true source. We consider four different sets of such allowed distortions, from time-invariant gains to time-varying filters. In each case, we decompose the estimated source into a true source part plus error terms corresponding to interferences, additive noise, and algorithmic artifacts. Then, we derive a global performance measure using an energy ratio, plus a separate performance measure for each error term. These measures are computed and discussed on the results of several BASS problems with various difficulty levels.

Index Terms—Audio source separation, evaluation, measure, performance, quality.

I. INTRODUCTION

BLIND audio source separation (BASS) has been a topic of intense work during the last years. Several successful models have emerged, such as independent component analysis (ICA) [1], sparse decompositions (SD) [2], and computational auditory scene analysis (CASA) [3]. However, it is still hard to evaluate an algorithm or to compare several algorithms because of the lack of appropriate performance measures and common test sounds, even in the very simple case of linear instantaneous mixtures. In this paper, we design new numerical performance criteria that can help evaluate and compare algorithms when applied on usual BASS problems. Before we present these, let us first describe the problems considered and discuss the existing performance measures and their drawbacks.

A. BASS General Notations

The BASS problem arises when one or several microphones record a sound that is the mixture of sounds coming from several sources. For simplicity, we consider here only linear time-invariant mixing systems. If we denote by $s_j(t)$ the signal emitted by the j th source ($1 \leq j \leq n$), $x_i(t)$ the signal recorded by the i th microphone ($1 \leq i \leq m$), and $a_{ij}(\tau)$ the (causal) source-to-

microphone filters, we have $x_i(t) = \sum_{j=1}^n \sum_{\tau=0}^{+\infty} a_{ij}(\tau) s_j(t-\tau) + n_i(t)$, where $n_i(t)$ is some additive sensor noise. This $m \times n$ mixture is expressed more conveniently using the matrix of filters formalism as

$$\mathbf{x} = \mathbf{A} \star \mathbf{s} + \mathbf{n} \quad (1)$$

where \star denotes convolution. In the following, variables without time index will denote batch sequences, e.g., $\mathbf{x} = [\mathbf{x}(0), \dots, \mathbf{x}(T-1)]$. Bold letters will be used for multichannel variables, such as the vector of observations \mathbf{x} , the vector of sources \mathbf{s} , or the mixing system \mathbf{A} , and plain letters for monochannel variables, such as the j th source s_j .

B. BASS Applications and Difficulty Levels

BASS covers many applications [4], and the criteria used to assess the performance of an algorithm depend on the application. Sometimes the goal is to extract source signals that are listened to, straight after separation or after some postprocessing audio treatment. Sometimes, it is to retrieve source features and/or mixing parameters to describe complex audio scenes in a way related to human hearing. In this paper, we focus on the most common task addressed by BASS algorithms: source extraction.

Source extraction consists in extracting from a mixture one or several mono source signals s_j . Examples include the denoising and dereverberation of speech for auditory protheses and the extraction of interesting sounds in musical excerpts for electronic music creation. Without specific prior information about the sources \mathbf{s} or the mixing system \mathbf{A} , this problem suffers from well-known theoretical indeterminacies [1], [5]. Generally, the sources can only be recovered up to a permutation and arbitrary gains, but further indeterminacies may exist in convolutive mixtures (e.g., up to a filter).

Source extraction can be addressed at various difficulty levels depending on the structure of the mixing system [6], [7]. A first difficulty criterion is the respective number of sources and sensors. In noiseless determined instantaneous mixtures (i.e., when $m = n$), there exists a time-invariant linear demixing system $\mathbf{W} = \mathbf{A}^{-1}$. After \mathbf{W} has been estimated, the sources can be simply recovered as $\mathbf{s} = \mathbf{W}\mathbf{x}$. In noiseless under-determined mixtures (i.e., when $m < n$), this is not possible anymore since the equation $\mathbf{x} = \mathbf{A}\mathbf{s}$ has an affine set of solutions. This non-trivial indeterminacy can be removed using knowledge about the sources, such as sparse priors [2]. A second difficulty criterion is the length of the mixing filters. Many algorithms for instantaneous noiseless determined mixtures provide near perfect results [1], [2], [8]. However, convolutive mixtures still raise challenging theoretical issues such as the identifiability of the sources up to gain and technical difficulties like the estimation of long mixing filters in short-duration mixtures.

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C. Existing Performance Measures and Their Limitations

Some performance measures for source extraction have already been defined in the literature. A first kind of measure assumes that the estimated sources $\hat{\mathbf{s}}$ have been recovered by applying a time-invariant linear demixing system \mathbf{W} to the observations \mathbf{x} . The global system $\mathbf{B} = \mathbf{W}\star\mathbf{A}$ verifies $\hat{\mathbf{s}} = \mathbf{B}\star\mathbf{s}$. The quality of \hat{s}_j is then measured by the row intersymbol interference [7]

$$\text{ISI}_j := \frac{\sum_{j',\tau} |B_{jj'}(\tau)|^2 - \max_{j',\tau} |B_{jj'}(\tau)|^2}{\max_{j',\tau} |B_{jj'}(\tau)|^2}. \quad (2)$$

ISI_j is always positive and equal to zero only when \hat{s}_j is equal to the true source $s_{j'}$ up to a gain and a delay τ with $(j',\tau) = \arg \max_{j',\tau} |B_{jj'}(\tau)|^2$. This criterion and other similar ones [9] are relevant, but cannot be applied to underdetermined BASS problems because a perfect time-invariant demixing system \mathbf{W} does not exist generally. Moreover, even in determined BASS, it is possible to use other separation schemes than time-invariant linear demixing. A second kind of measure consists in comparing directly \hat{s}_j and s_j , paying attention to the indeterminacies of the task. The gain indeterminacy can be handled by comparing L_2 -normalized versions of the sources with the relative square distance [2], [6], [10]

$$D := \min_{\epsilon=\pm 1} \left\| \frac{\hat{s}_j}{\|\hat{s}_j\|} - \epsilon \frac{s_j}{\|s_j\|} \right\|^2. \quad (3)$$

This measure is also relevant since it is always positive and equal to zero only when \hat{s}_j equals s_j up to a gain. However, D takes at most the value $D = 2$, even in the worst case, where the permutation indeterminacy has been badly solved and where \hat{s}_j equals another source $s_{j'}$ orthogonal to s_j . One would then desire a distortion $D = +\infty$. More generally, D evaluates bad results rather coarsely. For example, $\hat{s}_j = s_{j'}$ and $\hat{s}_j = s_{j'}/\|s_{j'}\| + 0.02s_j/\|s_j\|$ lead to similar measures $D = 2$ and $D \approx 1.96$ but are perceived quite differently.

These performance measures suffer from further limitations. Both consider only the case where \hat{s}_j has to be recovered up to a permutation and a gain. However, in some applications, it may be relevant to allow more or less distortions, not necessarily related to the theoretical indeterminacies of the problem. For example in hi-fi musical applications, it may be important to recover the sources up to a simple gain since arbitrary filtering modifies the timbre of musical instruments. On the contrary, in speech applications, some filtering distortion may be allowed because lowpass filtered speech is generally still intelligible. Moreover, both measures provide a single performance criterion containing all estimation errors. However, in audio applications, it is important to measure separately the amount of interferences from nonwanted sources, the amount or remaining sensor noise, and the amount of “burbling” artifacts (also termed “musical noise”). Such artifacts are often considered as a more annoying kind of error than interferences, that are themselves more annoying than sensor noise. Many separation methods for underdetermined BASS problems produce few interferences but many artifacts [11]–[13], and this cannot be described by a single criterion.

D. Overview of Our Proposals

The goal of this paper is to design new performance criteria that can be applied on all usual BASS problems and over-

come the limitations above. The only assumptions we make is as follows.

- The true source signals and noise signals (if any) are known.
- The user chooses a family of allowed distortions \mathcal{F} according to the application (but independently of the kind of mixture or the algorithm used).

The mixing system and the demixing technique do not need to be known.

Separate performance measures are computed for each estimated source \hat{s}_j by comparing it to a given true source s_j . Note that the measures do not take into account the permutation indeterminacy of BASS. If necessary, \hat{s}_j may be compared with all the sources $(s_{j'})_{1 \leq j' \leq n}$ and the “true source” may be selected as the one that gives the best results.

The computation of the criteria involves two successive steps. In a first step, we decompose \hat{s}_j as

$$\hat{s}_j = s_{\text{target}} + e_{\text{interf}} + e_{\text{noise}} + e_{\text{artif}} \quad (4)$$

where $s_{\text{target}} = f(s_j)$ is a version of s_j modified by an allowed distortion $f \in \mathcal{F}$, and where e_{interf} , e_{noise} , and e_{artif} are, respectively, the interferences, noise, and artifacts error terms. These four terms should represent the part of \hat{s}_j perceived as coming from the wanted source s_j , from other unwanted sources $(s_{j'})_{j' \neq j}$, from sensor noises $(n_i)_{1 \leq i \leq m}$, and from other causes (like forbidden distortions of the sources and/or “burbling” artifacts). In a second step, we compute energy ratios to evaluate the relative amount of each of these four terms either on the whole signal duration or on local frames.

E. Structure of the Paper

The rest of the paper has the following structure. In Section II, we show how to decompose \hat{s}_j and compute the performance measures when \mathcal{F} is the set of time-invariant gains distortions (this covers our preliminary proposals introduced in [14]). In Section III, we extend these results to the case where \mathcal{F} contains time-varying and/or filtering distortions. In Section IV, we test the measures on several BASS problems. In Section V, we discuss their relevance for algorithm evaluation and comment their correlation with subjective performance on informal listening tests. Finally, we conclude in Section VI by pointing out further perspectives about BASS evaluation and introducing our online evaluation database *BASS-dB* [15].

II. PERFORMANCE CRITERIA FOR TIME-INVARIANT GAINS ALLOWED DISTORTIONS

We propose in this section performance criteria for the most usual case when the only allowed distortions on \hat{s}_j are time-invariant gains. We first show how to decompose \hat{s}_j into four terms as in (4), and then we define relevant energy ratios between these terms.

Let us denote in the following $\langle a, b \rangle := \sum_{t=0}^{T-1} a(t)\bar{b}(t)$ the inner product between two possibly complex-valued¹ signals a and b of length T , where \bar{b} is the complex conjugate of b , and $\|a\|^2 := \langle a, a \rangle$ the energy of a .

¹Audio signals are real-valued, but it is costless to express our performance criteria in the slightly more general complex setting which might be useful for other types of signals.

A. Estimated Source Decomposition by Orthogonal Projections

When \mathbf{A} is a time-invariant instantaneous matrix and when the mixture is separated by applying a time-invariant instantaneous matrix \mathbf{W} , \hat{s}_j can be decomposed as

$$\hat{s}_j = (\mathbf{WA})_{jj}s_j + \sum_{j' \neq j} (\mathbf{WA})_{jj'}s_{j'} + \sum_{i=1}^m W_{ji}n_i. \quad (5)$$

Since $(\mathbf{WA})_{jj}$ is a time-invariant gain, it seems natural to identify the three terms of this sum with s_{target} , e_{interf} , and e_{noise} , respectively ($e_{\text{artif}} = 0$ here). However, (5) cannot be used as a definition of s_{target} , e_{interf} , e_{noise} , and e_{artif} since the mixing and demixing systems are unknown. Also, the two first terms of (5) may not be perceived as separate sound objects when a non-wanted source $s_{j'}$ is highly correlated with the wanted source s_j .

Instead, the decomposition we propose is based on orthogonal projections. Let us denote $\Pi\{y_1, \dots, y_k\}$ the orthogonal projector onto the subspace spanned by the vectors y_1, \dots, y_k . The projector is a $T \times T$ matrix, where T is the length of these vectors. We consider the three orthogonal projectors

$$P_{s_j} := \Pi\{s_j\} \quad (6)$$

$$P_{\mathbf{s}} := \Pi\{(s_{j'})_{1 \leq j' \leq n}\} \quad (7)$$

$$P_{\mathbf{s}, \mathbf{n}} := \Pi\{(s_{j'})_{1 \leq j' \leq n}, (n_i)_{1 \leq i \leq m}\} \quad (8)$$

and we decompose \hat{s}_j as the sum of the four terms

$$s_{\text{target}} := P_{s_j}\hat{s}_j \quad (9)$$

$$e_{\text{interf}} := P_{\mathbf{s}}\hat{s}_j - P_{s_j}\hat{s}_j \quad (10)$$

$$e_{\text{noise}} := P_{\mathbf{s}, \mathbf{n}}\hat{s}_j - P_{\mathbf{s}}\hat{s}_j \quad (11)$$

$$e_{\text{artif}} := \hat{s}_j - P_{\mathbf{s}, \mathbf{n}}\hat{s}_j. \quad (12)$$

The computation of s_{target} is straightforward since it involves only a simple inner product: $s_{\text{target}} = \langle \hat{s}_j, s_j \rangle s_j / \|s_j\|^2$. The computation of e_{interf} is a bit more complex. If the sources are mutually orthogonal, then $e_{\text{interf}} = \sum_{j' \neq j} \langle \hat{s}_j, s_{j'} \rangle s_{j'} / \|s_{j'}\|^2$. Otherwise, if we use a vector \mathbf{c} of coefficients such that $P_{\mathbf{s}}\hat{s}_j = \sum_{j'=1}^n \bar{c}_{j'} s_{j'} = \mathbf{c}^H \mathbf{s}$ (where $(\cdot)^H$ denotes Hermitian transposition), then $\mathbf{c} = \mathbf{R}_{\mathbf{ss}}^{-1} [\langle \hat{s}_j, s_1 \rangle, \dots, \langle \hat{s}_j, s_n \rangle]^H$, where $\mathbf{R}_{\mathbf{ss}}$ is the Gram matrix of the sources defined by $(\mathbf{R}_{\mathbf{ss}})_{jj'} = \langle s_j, s_{j'} \rangle$. The computation of $P_{\mathbf{s}, \mathbf{n}}$ proceeds in a similar fashion; however, most of the time we can make the assumption that the noise signals are mutually orthogonal and orthogonal to each source, so that $P_{\mathbf{s}, \mathbf{n}}\hat{s}_j \approx P_{\mathbf{s}}\hat{s}_j + \sum_{i=1}^m \langle \hat{s}_j, n_i \rangle n_i / \|n_i\|^2$.

B. From Estimated Source Decomposition to Global Performance Measures

Starting from the decomposition of \hat{s}_j in (6)–(12), we now define numerical performance criteria by computing energy ratios expressed in decibels. We define the source-to-distortion ratio

$$\text{SDR} := 10 \log_{10} \frac{\|s_{\text{target}}\|^2}{\|e_{\text{interf}} + e_{\text{noise}} + e_{\text{artif}}\|^2} \quad (13)$$

the source-to-interferences ratio

$$\text{SIR} := 10 \log_{10} \frac{\|s_{\text{target}}\|^2}{\|e_{\text{interf}}\|^2} \quad (14)$$

the sources-to-noise ratio

$$\text{SNR} := 10 \log_{10} \frac{\|s_{\text{target}} + e_{\text{interf}}\|^2}{\|e_{\text{noise}}\|^2} \quad (15)$$

and the sources-to-artifacts ratio

$$\text{SAR} := 10 \log_{10} \frac{\|s_{\text{target}} + e_{\text{interf}} + e_{\text{noise}}\|^2}{\|e_{\text{artif}}\|^2}. \quad (16)$$

These four measures are inspired by the usual definition of the SNR, with a few modifications. For instance, the definition of the SNR involving the term $s_{\text{target}} + e_{\text{interf}}$ at the numerator aims at making it independent of the SIR. Indeed, consider the case of an instantaneous noisy 2×2 mixture where $\hat{s}_1 = \epsilon s_1 + s_2 + e_{\text{noise}}$ with $\|\epsilon s_1\| \ll \|s_2\|$ and $\|e_{\text{noise}}\| \approx \|\epsilon s_1\|$. Then \hat{s}_1 is perceived as dominated by the interfering signal, with the noise energy making an insignificant contribution. This is consistent with $\text{SIR} \approx -\infty$ and $\text{SNR} \approx +\infty$ using our definitions. An SNR defined by $10 \log_{10} (\|s_{\text{target}}\|^2 / \|e_{\text{noise}}\|^2)$ would give $\text{SNR} \approx 0$ instead. Similarly, the SAR is independent of the SIR and the SNR since the numerator in (16) includes the interferences and noise terms as well.

Note that the numerical precision of the measures is lower for high-performance values than for low ones. For example, a high SDR means that the denominator in (13) is very small, so that small constant-amplitude errors in s_{target} (due to signal quantization) result in large SDR deviations. In particular, when the signals correspond to sound files, the precision of the results depends on the number of bits per sample.

C. Local Performance Measures

When the powers of s_{target} , e_{interf} , e_{noise} , and e_{artif} vary across time, the perceived separation quality also varies accordingly. We take this into account by defining local numerical performance measures in the following way.

First, we compute s_{target} , e_{interf} , e_{noise} , and e_{artif} as in (6)–(12). Then, denoting w a finite-length centered window, we compute the windowed signals s_{target}^r , e_{interf}^r , e_{noise}^r , and e_{artif}^r centered in r , where $s_{\text{target}}^r(t) = w(t-r)s_{\text{target}}(t)$, and so on. Finally, for each r , we compute the local measures SDR^r , SIR^r , SNR^r , and SAR^r as in (13)–(16) but replacing the original terms by the windowed terms centered in r .

SDR^r , SIR^r , SNR^r , and SAR^r , thus, measure the separation performance on the time frame centered in r . All these values can be visualized more globally by plotting them against r or by summarizing them into cumulative histograms [13]. Global performance measures can also be defined in the spirit of segmental SNR [16]. The shape of the window w has not much importance generally, only its duration is relevant. Thus, a rectangular window may be used for simplicity.

D. Comparison With Existing Performance Measures

The new performance measures solve most of the problems encountered with existing measures discussed in Section I-C.

First, the computation does not rely on the assumption that a particular type of demixing system or algorithm is used. The only assumption is that \hat{s}_j has to be recovered up to a time-invariant gain. Measures for other allowed distortions are proposed in Section III.

Second, the SDR has better properties than D . Simple calculus shows that both measures are identical up to a one-to-one mapping $10^{-\text{SDR}/10} = D(4-D)/(2-D)^2$. However, contrary to $-10 \log_{10} D$, the SDR is not lower-bounded: $\text{SDR} = -\infty$ when $s_{\text{target}} = 0$ and evaluation of bad results is less coarse [14].

Third, four criteria are proposed instead of a single one. The SIR, SNR, and SAR allow to distinguish between estimation errors that are mostly dominated by interferences, noise, or artifacts. This is verified on test mixtures in Section IV.

III. PERFORMANCE CRITERIA FOR OTHER ALLOWED DISTORTIONS

A. Which Equations Have to be Modified?

After having defined performance measures for time-invariant gains allowed distortions, we consider now similar measures for other allowed distortions. Much of the work done in the previous section is still relevant here and only the definitions of the orthogonal projectors in (6)–(8) have to be modified.

Indeed, the two steps consisting in decomposing \hat{s}_j in four terms and in computing energy ratios between these terms do not depend on each other. Since the kind of allowed distortion is not used in the second step, the performance measures are always defined by (13)–(16), whatever is the allowed distortion.

Moreover, the decomposition of \hat{s}_j can also often be defined by (9)–(12), but using other orthogonal projectors depending on the allowed distortions. In the following, we present successively the projectors used to decompose \hat{s}_j when filtering and/or time-varying distortions are allowed.

B. Time-Invariant Filters Allowed Distortions

When time-invariant filters are allowed, s_{target} is not a scaled version of s_j anymore, but a filtered version expressed as $s_{\text{target}}(t) = \sum_{\tau=0}^{L-1} h(\tau) \times s_j(t - \tau)$. If we express this in terms of subspaces, s_{target} does not generally belong to the subspace spanned by s_j but to the subspace spanned by delayed versions of s_j . So, we can define s_{target} by projecting \hat{s}_j on this new subspace.

We denote by s_j^τ and n_i^τ the source signal s_j and the noise signal n_i delayed by τ , so that $s_j^\tau(t) = s_j(t - \tau)$ and $n_i^\tau(t) = n_i(t - \tau)$. To avoid multiple definitions due to boundary effects, we consider the support of all signals to be $[0, T + L - 2]$, where $[0, T - 1]$ is the original support of the signals and $L - 1$ is the maximum delay allowed. We define the decomposition using the three projectors

$$P_{s_j} := \Pi \left\{ (s_j^\tau)_{0 \leq \tau \leq L-1} \right\} \quad (17)$$

$$P_s := \Pi \left\{ (s_{j'}^\tau)_{1 \leq j' \leq n, 0 \leq \tau \leq L-1} \right\} \quad (18)$$

$$P_{s,n} := \Pi \left\{ \left\{ (s_{j'}^\tau)_{1 \leq j' \leq n}, (n_i^\tau)_{1 \leq i \leq m} \right\}_{0 \leq \tau \leq L-1} \right\}. \quad (19)$$

The computation of the projections again involves inversion of Gram matrices. The Gram matrix corresponding to P_{s_j} is the empirical autocorrelation matrix of s_j defined by $(\mathbf{R}_{s_j s_j})_{\tau\tau'} = \langle s_j^\tau, s_j^{\tau'} \rangle$. The Gram matrix associated with P_s has a symmetric block-Toeplitz structure, where the blocks on the τ th diagonal are the empirical autocorrelation matrix of the sources at lag τ defined by $(\mathbf{R}_{ss}(\tau))_{jj'} = \langle s_j, s_{j'}^\tau \rangle$.

C. Time-Varying Gains Allowed Distortions

When time-varying gains distortions are allowed, s_{target} is equal to s_j multiplied by a slowly time-varying gain. We parameterize this gain as $g(t) = \sum_{u=0}^{U-1} \alpha_u v(t - uT')$, where v is

a positive kernel (i.e., a window) of length L' and T' the hop-size in samples between two successive “breakpoints.” When v is a rectangular window and $L' = T'$, this parameterization yields piecewise constant gains with breakpoints at uT' , but choosing a smoother kernel makes it possible to get more smoothly varying gains. This gives $s_{\text{target}}(t) = g(t)s_j(t) = \sum_{u=0}^{U-1} \alpha_u \times v(t - uT')s_j(t)$. Thus, s_{target} belongs to the subspace spanned by versions of s_j windowed by the kernel v . Note that this use of windowed source signals has no link with the computation of local performance measures from windowed decomposed signals in Section II-C. We emphasize again that the decomposition of \hat{s}_j and the computation of energy ratios are separate steps.

We define the windowed source signals $(s_j^u)_{0 \leq u \leq U-1}$ and the windowed noise signals $(n_i^u)_{0 \leq u \leq U-1}$ of support $[0, T - 1]$ by $s_j^u(t) = v(t - uT')s_j(t)$ and $n_i^u(t) = v(t - uT')n_i(t)$. The projectors for decomposition are given by

$$P_{s_j} := \Pi \left\{ (s_j^u)_{0 \leq u \leq U-1} \right\} \quad (20)$$

$$P_s := \Pi \left\{ (s_{j'}^u)_{1 \leq j' \leq n, 0 \leq u \leq U-1} \right\} \quad (21)$$

$$P_{s,n} := \Pi \left\{ \left\{ (s_{j'}^u)_{1 \leq j' \leq n}, (n_i^u)_{1 \leq i \leq m} \right\}_{0 \leq u \leq U-1} \right\}. \quad (22)$$

In order to guarantee the natural property $P_{s_j} s_j = s_j$ (i.e., $\text{SDR} = +\infty$ as expected in the particular case where $\hat{s}_j = s_j$), we enforce the condition that $\sum_{u=0}^{U-1} v(t - uT')$ is a constant for all t . When this is verified, s_j belongs to the subspace spanned by $(s_j^u)_{0 \leq u \leq U-1}$ because $s_j = \sum_{u=0}^{U-1} s_j^u / \sum_{u=0}^{U-1} v(t - uT')$. This condition always holds true when $T' = 1$, but other values of T' may work depending on the kernel v . For example, if v is a triangular window and L' is a multiple of 2, then $T' = L'/2$ also works.

D. Time-Varying Filters Allowed Distortions

Finally, when time-varying filters distortions are allowed, the decomposition of \hat{s}_j is made by combining the ideas of the two previous subsections. The estimated source s_{target} is expressed as a version of s_j “convolved” by a slowly time-varying filter. Using the notations of the previous subsections, this results in $s_{\text{target}}(t) = \sum_{\tau=0}^{L-1} h(\tau, t)s_j(t - \tau) = \sum_{\tau=0}^{L-1} \sum_{u=0}^{U-1} \alpha_{\tau u} \times v(t - uT')s_j(t - \tau)$. Thus, s_{target} belongs to the subspace spanned by delayed versions of s_j windowed by the kernel v .

We compute the windowed delayed source signals $(s_j^{\tau u})_{0 \leq \tau \leq L-1, 0 \leq u \leq U-1}$ and the windowed delayed noise signals $(n_i^{\tau u})_{0 \leq \tau \leq L-1, 0 \leq u \leq U-1}$ of support $[0, T + L - 2]$ by windowing delayed signals: $s_j^{\tau u}(t) = v(t - uT')s_j^\tau(t)$ and $n_i^{\tau u}(t) = v(t - uT')n_i^\tau(t)$. Note that the reverse order computation (passing windowed signals through delay lines) is not equivalent and results in other projections generally. We define the decomposition by the projectors

$$P_{s_j} := \Pi \left\{ (s_j^{\tau u})_{0 \leq \tau \leq L-1, 0 \leq u \leq U-1} \right\} \quad (23)$$

$$P_s := \Pi \left\{ (s_{j'}^{\tau u})_{1 \leq j' \leq n, 0 \leq \tau \leq L-1, 0 \leq u \leq U-1} \right\} \quad (24)$$

$$P_{s,n} := \Pi \left\{ \left\{ (s_{j'}^{\tau u})_{1 \leq j' \leq n}, (n_i^{\tau u})_{1 \leq i \leq m} \right\}_{0 \leq \tau \leq L-1, 0 \leq u \leq U-1} \right\}. \quad (25)$$

TABLE I
PARAMETER VALUES USED FOR DECOMPOSITION (8-kHz SAMPLE RATE)

Allowed distortion	Delays	Time frames		
	L	v	L'	T'
TI Gain	N/A	N/A		
TI Filt	256	N/A		
TV Filt	64	Rect	1600	1600

TABLE II
EVALUATION OF AN INSTANTANEOUS 2×2 MIXTURE

Method	Allowed distortion	SDR (dB)		SIR (dB)		SAR (dB)		SSIR (dB)	
		\hat{s}_1	\hat{s}_2	\hat{s}_1	\hat{s}_2	\hat{s}_1	\hat{s}_2	\hat{s}_1	\hat{s}_2
JADE	TI Gain	26	25	26	25	72	73	26	25
TFBSS	TI Gain	37	34	37	34	73	73	37	34

IV. EVALUATION EXAMPLES

In order to assess the relevance of our performance measures, we made tests on a few usual BASS problems. The separated sources were either simulated from a known decomposition or extracted from the mixtures with existing BASS algorithms.

In this section, we present the results of performance measurement on three noiseless mixtures of three musical sources. The sources are 16-bit sound files of 2.4 s, sampled at 8 kHz ($T = 19200$) and normalized. s_1 is cello, s_2 drums, and s_3 piano. The three mixtures are 16-bit sound files containing an instantaneous 2×2 mixture, a convolutive 2×2 mixture, and an instantaneous 2×3 mixture. These mixtures were chosen because they have very different difficulty levels, and they act as typical mixtures within the large amount of usual audio mixtures. We also chose some typical existing algorithms to separate these mixtures to show that the performance measures are relevant on “real life” data.

For each mixture and each algorithm, the (non quantized) estimated sources are decomposed using different allowed distortions and the performance measures are computed. The results are summarized in Tables II–IV. The different kinds of allowed distortions and corresponding decompositions are denoted TI Gain, TI Filt, TV Gain, and TV Filt, respectively. The values of the decomposition parameters are listed in Table I. Their choice is discussed in Section V based on informal listening tests.

The sound files corresponding to these examples are available for listening on <http://www.irisa.fr/metiss/demos/bssperf/>. This demo web page provides the sound files of the mixture \mathbf{x} , the sources \mathbf{s} , the first estimated source \hat{s}_1 , and also the sound files of s_{target} , e_{interf} , e_{noise} , and e_{artif} from the decomposition of \hat{s}_1 . Sound files of \hat{s}_2 , \hat{s}_3 and their decompositions are not provided for the sake of legibility. We emphasize that listening to these sounds and comparing with the related performance figures is the best way to evaluate the meaningfulness of our proposals.

A. Instantaneous 2×2 Mixture

Our first example is a stereo instantaneous mixture of s_1 and s_2 , obtained with the mixing matrix

$$\mathbf{A} = \begin{bmatrix} 0.5 & 1 \\ 1 & 0.5 \end{bmatrix}.$$

We solve this problem by estimating a demixing matrix with two different ICA methods: by using non Gaussian distributions and mutual independence of the sources with JADE [1], and by finding zones in the time–frequency plane where only one source is present with time–frequency blind source separation (TFBSS) [8] (used with 64 time frames and 1024 frequency bins as input parameters). The performance measures are shown in Table II for TI Gain decompositions. Results with other decompositions differ from less than 2 dB. Since the global mixing–unmixing system \mathbf{WA} is known, we also compute for comparison the System SIR (SSIR) which is the power ratio between the two first terms of (5).

As expected with sources estimated by time-invariant linear demixing, no artifacts come into play: $\text{SAR} \approx +\infty$ up to numerical precision. The estimation error is dominated by interferences and $\text{SDR} \approx \text{SIR}$. Moreover, the SIR is higher for TFBSS than for JADE. This result is corroborated by the fact that the demixing matrix estimated with TFBSS is closer to the true demixing matrix than with JADE. Also, as expected, the SSIR is very close to the SIR, because the correlation between the sources $\langle s_1, s_2 \rangle = -0.0055$ is small.

B. Convolutive 2×2 Mixture

Our second example is a convolutive mixture of s_1 and s_2 made with 256 tap filters. The problem is solved by a frequential domain ICA method using 256 subbands and separating the mixture with JADE [1] in each subband. The usual “permutation problem” [5] is encountered when building estimated sources from extraction results in each subband. We test two methods to address this problem: the method outlined in [5] and an oracle (i.e., choice of the optimal permutations knowing the true sources). The corresponding algorithms are named frequential ICA (FICA) or oracle frequential ICA (OFICA). Both methods do not aim at recovering the sources s_1 and s_2 , but their images on the first channel $a_{11} \star s_1$ and $a_{12} \star s_2$. Thus, the estimated sources may be at best filtered versions of the true sources. The performance measures are shown in Table III for three different decompositions. We compute again the SSIR from (5), with \mathbf{WA} now containing filters instead of gains.

Different conclusions arise depending on the decomposition. The TI Gain decomposition results in low SDRs for both methods and $\text{SDR} \approx \text{SAR}$. Many artifacts arise due to forbidden (filter) distortions of the sources. On the contrary, the TI Filt decomposition outputs a high SDR for OFICA and a medium SDR for FICA with $\text{SDR} \approx \text{SIR}$. Artifacts are smaller because filter distortions are allowed, and interferences are larger for FICA than for OFICA, because the use of oracle information in OFICA prevents bad pairing of subbands. The TV Filt decomposition leads to intermediate results. Short (64-tap) filter distortions are allowed, but longer filter distortions are not; thus, some of the filter distortions on the estimated sources are counted toward artifacts. Again, the SSIR is very close the SIR computed using the TI Filt decomposition, because the

TABLE III
EVALUATION OF A CONVOLUTIVE 2×2 MIXTURE

Method	Allowed distortion	SDR (dB)		SIR (dB)		SAR (dB)		SSIR (dB)	
		\hat{s}_1	\hat{s}_2	\hat{s}_1	\hat{s}_2	\hat{s}_1	\hat{s}_2	\hat{s}_1	\hat{s}_2
FICA	TI Gain	-11	-16	7	12	-10	-16		
	TI Filt	6	14	6	17	19	17	6	16
	TV Filt	3	-2	8	9	5	-1		
OFICA	TI Gain	-10	-13	15	22	-10	-13		
	TI Filt	10	16	10	18	19	19	10	17
	TV Filt	5	-2	15	10	5	-1		

TABLE IV
EVALUATION OF AN INSTANTANEOUS 2×3 MIXTURE

Method	Allowed distortion	SDR (dB)			SIR (dB)			SAR (dB)		
		\hat{s}_1	\hat{s}_2	\hat{s}_3	\hat{s}_1	\hat{s}_2	\hat{s}_3	\hat{s}_1	\hat{s}_2	\hat{s}_3
STFTC	TI Gain	2	4	4	15	9	29	3	7	4
	TI Filt	5	4	6	14	7	19	6	8	6
	TV Filt	6	5	8	11	7	15	8	11	9
MPC	TI Gain	4	8	15	19	27	31	4	8	15
	TI Filt	5	9	16	13	17	27	5	9	16
	TV Filt	6	9	16	14	14	23	7	11	17

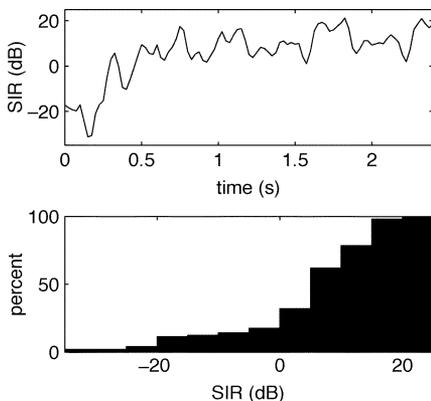


Fig. 1. Local SIR for \hat{s}_1 estimated by FICA and TI Filt decomposition in the 2×2 convolutive mixture. Hanning windows of length 100 ms and overlapping 75 ms are used. The SIR is plotted against time in the upper plot and summarized in a cumulative histogram in the lower plot.

correlation between delayed versions of different sources is also small.

It is also interesting to study the evolution of the performance measures across time. For example, Fig. 1 plots the local SIR for \hat{s}_1 (estimated with FICA) using TI Filt. We see that the actual performance measure varies a lot, which cannot be explained by a single global SIR.

C. Instantaneous 2×3 Mixture

Our third example is an instantaneous mixture of s_1 , s_2 , and s_3 computed with the mixing matrix

$$\mathbf{A} \approx \begin{bmatrix} 0.92 & 1.40 & 1.05 \\ 0.36 & 1.30 & 2.36 \end{bmatrix}.$$

To solve this problem, we represent the two mixture channels in a domain where the sources exhibit a sparse behavior, and then the mixing matrix and the sources are estimated by (non-linear) clustering of the ratios of the representation coefficients between the channels. Two algorithms are tested: a clustering of the short-time Fourier transform (STFT) called DUET [12] (using a 256-sample Hanning window and a 192-sample hop-size for STFT computation) and a matching pursuit clustering (MPC) [11] (using 10 000 Gabor atoms with truncated Gaussian envelope). The performance measures are shown in Table IV

for two different decompositions. Unlike in the previous experiments, it does not seem possible to display any sort of ‘‘System SIR’’ for the MPC algorithm, since the result of the separation is not a linear function of the input sources. In a sense, this perfectly illustrates a situation where it is necessary to have at hand performance measures such as the ones we define, that is to say measures which do not rely on a particular type of separation algorithm, but simply try to compare the estimated signals with the target ones.

This time the choice of the decomposition has less influence on the results. Both methods estimate the sources essentially without filter distortions but with ‘‘burbling’’ artifacts due to source overlap in the representation domain. Thus, SDRs are low for both methods and $\text{SDR} \approx \text{SAR}$. Note that MPC leads to better performance than DUET, particularly for \hat{s}_3 . Indeed, the use of an overcomplete dictionary in MPC makes the source representations sparser and limits source overlap.

V. DISCUSSION

Before we conclude, let us summarize in this section the results of the evaluation examples. We discuss the relevance of the proposed performance measures for algorithm evaluation and comparison. Then, we describe how they could possibly be modified to explain subjective auditory assessments.

A. Relevance for Algorithm Evaluation and Comparison

The main result of the previous section is that the SDR, SIR, SNR, and SAR were found to be relevant for the evaluation of an algorithm and the comparison of several algorithms. Indeed, given a family of allowed distortions, the SIR and SAR were shown to be valid performance measures regarding two separate goals: rejection of the interferences and absence of forbidden distortions and ‘‘burbling’’ artifacts. Other experiments proved that the SNR was also valid for a third goal: rejection of the sensor noise. Finally, the SDR was shown to be valid as a global performance measure in case these three goals are equally important.

Another important result is that the measures were found to depend a lot on the number of delays and time frames chosen for decomposition. Experimentally, the more distortions are allowed, the higher the SDRs are. More rigorously, when \mathcal{F} and \mathcal{F}' are two families with $\mathcal{F} \subset \mathcal{F}'$, the SDR of a given estimated

source \hat{s}_j is higher allowing distortions in \mathcal{F}' than in \mathcal{F} . Indeed, the projection subspaces verify $\{f(s_j), f \in \mathcal{F}\} \subset \{f(s_j), f \in \mathcal{F}'\}$, and, thus, $\|\hat{s}_j - P_{s_j}\hat{s}_j\|$ is smaller allowing distortions in \mathcal{F}' than in \mathcal{F} .

This confirms our main postulate that the evaluation of the performance of an algorithm only makes sense given a family of allowed distortions. This can be seen as a nice property if the distortions allowed for the desired application correspond to one of the families presented in Sections II and III with a precisely known number of frequency subbands and time frames. However, this is annoying when one has no idea about which distortions to allow. In that case, we cannot “recommend” a family of allowed distortions more than another one: the “best” choice really depends on the application.

Finally, an interesting result is that in the previous section, the results of algorithm classification according to mean SDR were always the same whatever decomposition was used. We make the hypothesis that this is not a coincidence and that the classification order is rather independent of the family of allowed distortions. Of course, this hypothesis is based on very few experiments actually, but we think it would be interesting to validate or infirm it using more data. If it was true, then algorithm classification would be greatly simplified. Indeed, it would be unnecessary to test many families of allowed distortions before providing a global result: a single one would suffice.

B. Relevance Toward Subjective Performance Measures

Another interesting question is to study the relationship between the proposed measures and subjective auditory performance assessments. In theory, this should be done using carefully calibrated psychoacoustical listening tests. We could first ask the listeners how they describe the results with their own words, and check whether they use synonyms of “interferences” and “artifacts” or not. Then we could go on with more constrained tests, such as broadcasting pairs of results and asking listeners if they hear more or less “interferences” and “artifacts” in the first sound of each pair. Because performing these listening tests is not a trivial task, we give here only a few remarks based on our own listening experience.

If we admit that the ear splits estimated sources into the same four components than our analytical decomposition, we may define interferences, noise and artifacts as “what I hear coming from the other sources,” “what I hear coming from sensor noise,” and “what I hear to be burbling artifacts.” With this definition of auditory performance measures, we remark that the SIR, SNR, and SAR seem to be better related to the auditory notion of interferences, noise, and artifacts using the TV Filt decomposition. Indeed, decompositions using very few delays and time frames are not always able to extract all the perceived interferences inside e_{interf} but split them between e_{interf} and e_{artif} . On the contrary, decompositions with too many delays and/or time frames sometimes put “burbling” artifacts into e_{interf} and nothing into e_{artif} . The parameters we chose for the TV Filt decomposition ($F' = 64$ and $L' = 200$ ms) appear to be a good compromise in many experiments. When the TI Filt decomposition is used, a higher number of delays ($L = 256$) seems preferable. Of course, these choices cannot be proved using physical or mathematical arguments, but readers may check this partially by listening to the previous examples on <http://www.irisa.fr/metiss/demos/bssperf/>.

If we also admit that the ear associates energy prioritarily to the true source rather than to interferences in the case where some sources are similar, then the components s_{target} , e_{interf} , e_{noise} , and e_{artif} estimated by the “greedy” decomposition of (9)–(12) should be closer to the perceptual components than those estimated by the simultaneous decomposition of (5). Indeed, the “greedy” decomposition scheme takes into account similarity between sources as measured by correlation. We think that this measures part of the perceptual similarity between sources, but not all. For instance, two white noises sound the same even when they are orthogonal.

Some other auditory properties cannot be explained by the proposed measures. First, the high values of SIR, SNR, and SAR have limited auditory signification. For example, the two instantaneous mixtures of Section IV-A have very different SIRs but can hardly be distinguished. Also, the SDR does not measure the total perceived distortion. In the case where \hat{s}_j is a slightly lowpass filtered version of s_j , then $\text{SDR} \approx +\infty$ using TV Filt decomposition but lowpass filtering is perceived as timbre distortion. This fourth kind of error (besides interferences, noise, and “burbling” artifacts) could be dealt with using an additional performance measure, such as Itakura–Saito distance or cepstral distortion [16].

An interesting idea to mimic the auditory treatments would be to pass the sources and noises through an auditory filter bank. Then each estimated source could be decomposed on subspaces spanned by the auditory subbands by handling differently sinusoidal and noise-like zones and by taking into account auditory masking phenomena. Similar performance measures already exist in the fields of denoising and compression [13], [17].

VI. CONCLUSION AND PERSPECTIVES

In this paper, we discussed the question of performance measurement in BASS. Given a set of allowed distortions, we evaluated the quality of an estimated source by four measures called SDR, SIR, SNR, and SAR. Experiments involving typical mixtures and existing algorithms showed that these measures were relevant for algorithm evaluation and comparison. With respect to other existing performance measures, the main improvement is that we do not assume a particular separation algorithm nor a limited set of allowed distortions. Moreover, we evaluate separately the amount of interferences, remaining sensor noise, and artifacts, which is a crucial point for evaluation in underdetermined mixtures.

Our performance measures are implemented within a MATLAB toolbox named *BSS_EVAL* distributed online under the GNU Public License [18].

The main application of this work is to rank existing BASS algorithms according to their performance on the same test data. To help this, we built a web database called *BASS-dB* [15] that classifies the test mixtures according to the source extraction subtasks [4]. These subtasks corresponds to different structures of the mixing system defined by the number of sources and sensors (2×2 , 2×5 , 5×5 , 7×5 , etc.) and the kind of mixing filters (gain, delay, gain + delay, live-recorded room impulse responses). *BASS-dB* already provides some test mixtures and performance results, but we encourage people to feed it with their own mixtures and results.

We hope the BASS community will consider this issue, so that BASS methods can be compared within a shared framework.

Among the results, the best BASS methods could be identified and selected for further improvement, or objective difficulty criteria could be defined to determine for example whether the difficulty in an underdetermined convolutive mixture rather comes from convolution or from underdetermination. Our hypothesis that algorithm classification results are rather independent of allowed distortions could also be validated or infirmed.

Among the possible generalizations to this paper, we are currently studying the derivation of psychoacoustical performance measures and performance measures for the similar BASS tasks of source spatial image extraction and remixing [4], that also involve listening to the extracted sources.

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