

Multiagent epistemic planning

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The importance of reasoning about knowledge and belief

- S. Baron Cohen's False-belief-tasks (Sally-Ann Test, ...)

[S. Baron Cohen 1985]

<https://www.youtube.com/watch?v=jbL34F81Rz0>

- <https://www.youtube.com/watch?v=N6y1H-LYj0M>

- typically fail the test:

- children under 3
- autistic children

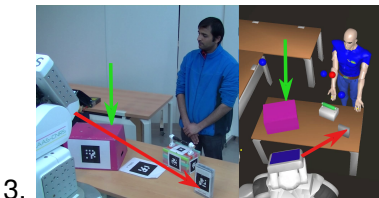
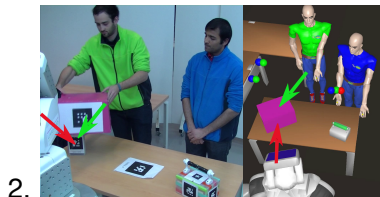
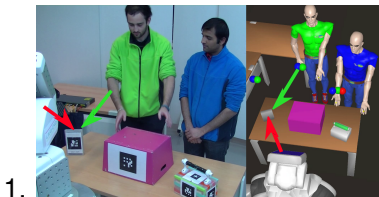
- hypothesis: specific human capacity of reasoning about other agents' beliefs ('mind reading', '*theory of mind*')

- relevant for any interaction with a human being
- specifically: planning future actions involving others

- epistemic reasoning = reasoning about knowledge and belief (large sense)

Challenge: robots with theory of mind [Milliez et al. 2014]

- at step 3, GREEN's beliefs become false
 - colored arrows = beliefs about white book position (red = robot)
 - colored spheres = reachability of an object for an agent



Epistemic reasoning in planning

1 single-agent planning

- uncertainty about initial situation
- uncertainty about action effects
- sensing actions (alias knowledge producing actions)

⇒ contingent/conformant planning

2 multiagent planning

- initial situation

first-order: *I don't know whether p.*

second-order: *I don't know whether you know that p.*

I know that you don't know whether p.

...

- goal

first-order: *I want to know whether p.*

second-order: *I want to know whether you know that p.*

I want you to know that q.

third-order: ...

- actions

- have epistemic effects: sensing, communication

Problems, problems

- representation problems:
 - model ‘expiry date’ for knowledge/belief?
 - light in room x is on at time point T
 - j is in room x (so j believes that the light is on at T)
 - j leaves the room at $T+1$
 - at $T' > T$, does j still believe that the light in x is on?
 - higher-order belief revision?
 - simple integrations of epistemic and spatial reasoning?
- ⇒ to be solved in any application!
- reasoning problems:
 - epistemic reasoning is difficult
 - at least PSPACE (just as classical planning)
 - EXPTIME complete if common knowledge/belief involved
 - no ‘epistemic planning’s blocksworld’ (yet)
 - no good benchmarks (yet)

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Outline

- 1 What's in a planning problem?
- 2 States and goals: Epistemic Logic
- 3 Actions and plans: Dynamic Epistemic Logic
- 4 The simplest multiagent epistemic planning problem: gossiping
- 5 Observability-based knowledge
- 6 Epistemic planning with conditional effects
- 7 Embeddings

What's in a planning problem?

planning problem = $\langle \text{init}, \text{goal}, \text{actionLaws} \rangle$

- 1 logical form of `init`: proposition
 - proposition = set of states ('possible worlds')
 - can be described in various logical languages:
 - propositional logic
 - epistemic logic
 - ...
 - classical planning:
 - initial state = a single possible world
 - = a valuation of propositional logic
 - = complete proposition
- 2 logical form of `goal`: proposition
- 3 logical form of `actionLaws`: action *type*
 - action type: *arm-raising*
 - action token: *Paulo's raising of his right arm in room 7 of building 007 on Oct. 1, 2018 at 11:55:55*

What's in an action?

- “something that has precondition and effects” [AI folklore]

action = \langle precond, effect \rangle

- precondition = proposition
- effect = ?

What's in an action effect?

- STRIPS actions: effect = conjunction of literals
- however: an action type is instantiated in different circumstances \Rightarrow effects typically depend on these circumstances
- conditional effects:

$$\text{effect} = \left\{ \langle \text{condition}_1, L_{1,1} \wedge \dots \wedge L_{1,m_1} \rangle, \right. \\ \dots, \\ \left. \langle \text{condition}_n, L_{n,1} \wedge \dots \wedge L_{n,m_1} \rangle \right\}$$

- example: agent i 's action of flipping a switch

$$\text{precond}(\text{flip}_i) = \text{AtSwitch}_i$$

$$\text{effect}(\text{flip}_i) = \{ \langle \neg \text{On}, \text{On} \rangle, \\ \langle \text{On}, \neg \text{On} \rangle \}$$

- what about epistemic effects?

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Epistemic logic: language

- $K_i\varphi$ = “agent i knows that φ ”
- grammar:

$$\varphi ::= p \mid \neg\varphi \mid \varphi \wedge \varphi \mid K_i\varphi$$

where p ranges over **Prp** and i over **Agt**

- first-order epistemic attitudes w.r.t. p :

$K_i p$	$K_i \neg p$	$\neg K_i p \wedge \neg K_i \neg p$
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- second-order attitudes:

$K_i p \wedge K_i K_j p$	$K_i \neg p \wedge K_i K_j \neg p$	$(\neg K_i p \wedge \neg K_i \neg p) \wedge K_i(\neg K_j p \wedge \neg K_j \neg p)$
$K_i p \wedge K_i(\neg K_j p \wedge \neg K_j \neg p)$...	$(\neg K_i p \wedge \neg K_i \neg p) \wedge K_i(K_j p \vee K_j \neg p)$
$K_i p \wedge (\neg K_i K_j p \wedge \neg K_i \neg K_j p)$...	\emptyset

Epistemic logic: possible worlds semantics

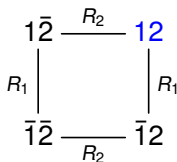
- knowledge explained in terms of possible worlds [Hintikka 1962]:

“agent i knows that φ ” = φ true in every world that is possible for i

- model $M = (W, \{R_i\}_{i \in \text{Agt}}, V)$ with
 - W non-empty set of possible worlds
 - $R_i \subseteq W \times W$ accessibility relations
 - $V : W \rightarrow 2^{\text{Prp}}$ valuation
- R_i is an equivalence relation (indistinguishability)
 - $R_i(w)$ = “set of worlds i cannot distinguish from w ”
 - = “set of worlds compatible with i ’s knowledge”
- truth conditions:
 - $M, w \models p$ iff $p \in V(w)$
 - $M, w \models \neg\varphi$ iff ...
 - $M, w \models \varphi \wedge \psi$ iff ...
 - $M, w \models K_i\varphi$ iff $M, w' \models \varphi$ for all $w' \in R_i(w)$

Epistemic logic: possible worlds semantics

- muddy children puzzle, initial situation



(reflexive arrows omitted)

$$M, 12 \models m_1 \wedge m_2 \wedge K_1 m_2 \wedge \neg K_1 m_1 \wedge \neg K_1 \neg m_1$$

Epistemic logic for epistemic planning?

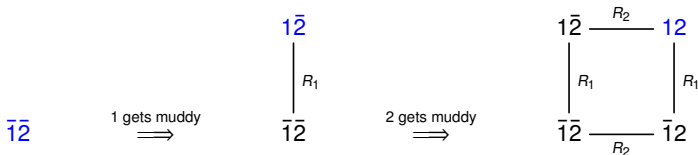
- can be modeled:
 - `init` = formula of epistemic logic
 - `goal` = formula of epistemic logic
- cannot be expressed:
 - `actionLaws`

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Muddy children: Episode 1

- 1 initially, common knowledge that nobody is muddy
- 2 1 gets muddy but isn't sure; 2 watches
- 3 2 gets muddy but isn't sure; 1 watches



Dynamic epistemic logic DEL

- idea: model uncertainty about *current event* by introducing *possible events*

uncertainty about world	uncertainty about event
possible worlds	possible events
indistinguishability of worlds	indistinguishability of events

⇒ ‘possible event models’

- distinguish agents who observe from agents who don’t
N.B.: an agent typically observes only very few events
- muddy children:
event model where 1 plays, 2 watches

$skip_1 \xrightarrow{R_1} getsMuddy_1$

(reflexive arrows omitted)

DEL: event models

- $EM = (E, \{S_i\}_{i \in \mathbf{Agt}}, \text{precond}, \text{effect})$ event model, where
 - E is a nonempty set of events
 - $S_i \subseteq E \times E$
 - every S_i is an equivalence relation
 - $eS_i f =$ “ i perceives occurrence of e as occurrence of f ”
 - $\text{precond} : E \rightarrow \text{Fmls}$
 - $\text{effect} : E \rightarrow \text{Fmls}$ s.th. $\text{effect}(e)$ conjunction of literals
(just as in STRIPS)

DEL: product construction

- update world model $WM = (W, R, V)$ by event model EM

$$WM \otimes EM = WM'$$

where

$$\begin{aligned} W' &= \{(w, e) \in W \times E : M, w \models \text{precond}(e)\} \\ (w, e)R'_i(v, f) &\text{ iff } wR_i v \text{ and } eS_i f \\ V'((w, e)) &= (V(w) \setminus \{p : p \text{ negative in effect}(e)\}) \\ &\quad \cup \{p : p \text{ positive in effect}(e)\} \end{aligned}$$

DEL for epistemic planning?

- explored since >5 years [Bolander&Anderson 2011]; [Löwe, Pacuit&Witzel 2011]; [Aucher, Maubert&Pinchinat 2014]; [Yu, Li&Wang 2015],...
- `init` = formula of multiagent epistemic logic
- `goal` = formula of multiagent epistemic logic
- `action type` = agent + event model
- reasoning: not so easy
 - plan existence undecidable in general [Bolander&Anderson 2011]; [Aucher&Bolander 2013]; [Charrier, Maubert&Schwarzentruber 2016]
 - decidable fragments: heavily restricted [Yu, Wen&Liu 2013]; [Bolander et al. 2015],...
 - world models typically grow exponentially when updated
- representation: some problems that seemingly went unnoticed...

DEL for epistemic planning: problems

- event models rather describe action tokens
- `actionLaws` describe types, not tokens
- how to describe conditional effects?
 - list all possible cases of perception of the actual event
 - infinitely many conditional effects needed
- conditional effects of `getMuddy(i)`:

$$(\top, m_i)$$

$$(inGarden_j, K_j m_i)$$

$$(K_j inGarden_j, K_j(K_j m_i \vee K_j \neg m_i))$$

$$(K_j K_j inGarden_j, \dots)$$

$$\vdots$$

$$(CK_{i,j} inGarden_j, CK_{i,j}(K_j m_i \vee K_j \neg m_i))$$

⇒ event model with an infinite number of points!

- even when finite, event models have to be big

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The gossip problem

- [Baker&Shostak, Discrete Mathematics 1972]
- n friends
- each friend i has a secret Σ_i
- two friends can call each other to exchange all the secrets they know
- how many calls to spread all secrets among all friends?



The gossip problem

- relevant for distributed database, social networks, disease spreading, . . .
- hot topic in the DEL community
- different kinds of protocols; here:
 - complete graph
 - other graphs:
[Cooper et al., Discrete Maths, to appear]
 - centralized protocol
 - distributed variants:
[Apt et al., TARK 2016; IJCAI 2017]
[van Ditmarsch et al., LOFT 2016]
- paradigmatic epistemic planning problem?
 - ‘multiagent planning’s blocksworld’



The gossip problem: solution

- initial state: $\left(\bigwedge_{1 \leq i \leq n} K_i \Sigma_i \right) \wedge \left(\bigwedge_{1 \leq i, j \leq n, j \neq i} \neg K_i \Sigma_j \right)$
- goal: shared knowledge ('everybody knows')

$$EK \text{ AllSecrets} = \bigwedge_{1 \leq i \leq n} K_i \left(\bigwedge_{1 \leq j \leq n} \Sigma_j \right)$$

- naive algorithm: $2(n-1)$ calls
- optimal algorithm:

friends	calls
2	1
3	3
4	4
5	6
6	8
⋮	⋮
$n \geq 4$	$2(n-2)$



The gossip problem: attaining higher-order shared knowledge

- attain shared knowledge of level k :

$$\underbrace{EK \dots EK}_{k \text{ times}} \text{ AllSecrets}$$

N.B.: impossible to obtain common knowledge (cf. Byzantine Generals)

- algorithm with calls to attain shared knowledge of order k

[Herzig&Maffre, AI Commun. 2017]

friends	calls for $k=1$	calls for $k=2$...
2	1	1	
3	3	4	
4	4	6	
⋮	⋮	⋮	⋮
$n \geq 4$	$2 \times (n-2)$	$3 \times (n-2)$	

- for $n \geq 4$ and $k \geq 1$: $(k+1) \times (n-2)$ calls
- optimal [Cooper et al., ECAI 2016; Discrete Maths, to appear]

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Grounding knowledge on propositional observability

agent i observes whether propositional variable p is true

- originates in model checking distributed systems (MOCHA)
 - logic:
[v.d.Hoek&Wooldridge, AIJ 2005; v.d.Hoek et al., AAMAS 2011]
- *derive* indistinguishability relation:
$$R_i = \{(s, s') : s(p) = s'(p) \text{ for every } p \in PVar \text{ observed by } i\}$$
- interpret epistemic operator in Kripke model $(2^{PVar}, R, id)$
- **compact models**
 - 1 valuations of classical propositional logic
 - 2 visibility information: subset of $\mathbf{Agt} \times \mathbf{Prp}$
- ‘anti-Hintikka’
 - grounded on origins of knowledge (what we know comes from observation + communication)

Propositional observability: properties

$i \text{ observes } p \text{ iff } K_i p \vee K_i \neg p \text{ true}$

- all axiom schemas of S5 valid
- plus some more:
 - ☹ distributes over disjunction:

$$K_i(p \vee q) \leftrightarrow (K_i p \vee K_i q)$$

- ☹ who observes what is common knowledge:

$$(K_i p \vee K_i \neg p) \rightarrow K_j(K_i p \vee K_i \neg p)$$

$$\neg(K_i p \vee K_i \neg p) \rightarrow K_j \neg(K_i p \vee K_i \neg p)$$

⇒ not appropriate for gossiping!

Higher-order observability

- idea: introduce **higher-order visibility atoms**

$S_i p$ = “ i sees the value of p ”

$S_i S_j p$ = “ i sees *whether* j sees the value of p ”

$S_i S_j S_k p$ = “...”

- intuitively:

$$K_i p \leftrightarrow p \wedge S_i p$$

$$K_i \neg p \leftrightarrow \neg p \wedge S_i p$$

$$K_i K_j p \leftrightarrow K_i (p \wedge S_j p)$$

$$\leftrightarrow K_i p \wedge K_i S_j p$$

$$\leftrightarrow p \wedge S_i p \wedge S_j p \wedge S_i S_j p$$

Language

- grammar:

$$\varphi ::= \sigma p \mid \neg\varphi \mid \varphi \wedge \varphi \mid K_i\varphi$$

where σp is a *visibility atom*

- σ = sequence of visibility operators S_i
- p = propositional variable
- propositional variables are special cases: σ empty

States

- state s = set of visibility atoms
 - initial gossip state (supposing all secrets are true)

$$s_0 = \{\Sigma_1, \dots, \Sigma_n\} \cup \{S_1 \Sigma_1, \dots, S_n \Sigma_n\}$$

- define indistinguishability relations as before:

$$sR_i s' \quad \text{iff} \quad \forall \alpha, \text{ if } S_i \alpha \in s \text{ then } s(\alpha) = s'(\alpha)$$

- problem: reflexive, but neither transitive nor symmetric
 - $\emptyset R_i s$ for every s
 - not $(sR_i \emptyset)$ as soon as $p \in s$ and $S_i p \in s$
- s must be **introspective**
 - contains all observability atoms of form $\sigma S_i S_i \sigma' p$, for all i
- properties of introspective states:
 - R_i equivalence relations
 - who observes what no longer common knowledge
 - $S_i p \rightarrow S_j S_i p$ invalid
 - $S_i p \rightarrow K_j S_i p$ invalid
 - $(K_i p \vee K_i \neg p) \rightarrow K_j (K_i p \vee K_i \neg p)$ invalid
- **normal form**: replace $\sigma S_i S_i \sigma' p$ by \top (introspectively valid)

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Conditional actions

- *conditional action* $a = (pre(a), eff(a))$ where:
 - $pre(a)$ proposition
 - $eff(a)$ set of conditional effects; in particular:
 - add observability atoms
 - delete observability atoms
- example:

$$pre(call_j^i) = \top$$

$$eff(call_j^i) = \{(S_i \Sigma_1 \vee S_j \Sigma_1, \{S_i \Sigma_1, S_j \Sigma_1\}, \emptyset),$$

...

$$(S_i \Sigma_n \vee S_j \Sigma_n, \{S_i \Sigma_n, S_j \Sigma_n\}, \emptyset)\}$$

- conditional action $a \Rightarrow$ transition relation between states R_a

Conditional actions: normal form

- $a = (pre(a), eff(a))$ is in normal form iff
 - ① $pre(a)$ in normal form
 - no introspectively valid $\sigma S_i S_i \sigma' p$
 - ② every conditional effect $ce \in eff(a)$ in normal form
 - ③ no conflicting effects
- every action can be put in normal form

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Planning tasks

- planning task = $(Act, s_0, goal)$ where
 - Act is a finite set of actions
 - s_0 finite state (the initial state)
 - $goal \in Fmls_{bool}$
- is in *normal form* iff
 - ...
- is *solvable* if there is a state s such that
 - 1 $s_0 \left(\bigcup_{a \in Act} R_a \right)^* s$
 - 2 $s \models goal$

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Extending the logic by assignment programs

- extend logic of observability-based knowledge by assignment programs

$$\varphi ::= \sigma p \mid \neg \varphi \mid \varphi \wedge \varphi \mid K_i \varphi \mid [\pi] \varphi$$

$$\pi ::= +\sigma p \mid -\sigma p \mid \pi; \pi \mid \pi \sqcup \pi \mid \pi^* \mid \varphi?$$

- call = program:

$$\text{call}_j^i = ((K_i \Sigma_1 \vee K_j \Sigma_1?; +S_i \Sigma_1; +S_j \Sigma_1) \sqcup \neg(K_i \Sigma_1 \vee K_j \Sigma_1?));$$

⋯ ;

$$((K_i \Sigma_n \vee K_j \Sigma_n?; +S_i \Sigma_n; +S_j \Sigma_n) \sqcup \neg(K_i \Sigma_n \vee K_j \Sigma_n?))$$

- For initial gossip state s_0 :

$$s_0 \models [\text{call}_2^1; \text{call}_4^3; \text{call}_6^5; \text{call}_3^1; \text{call}_5^4; \text{call}_6^1; \text{call}_4^2; \text{call}_5^3] EK \text{ AllSecrets}$$

$$s_0 \models \left\langle \left(\bigsqcup_{1 \leq i, j \leq 6} \neg S_i \Sigma_j?; \text{call}_j^i \right)^6 \right\rangle EK \text{ AllSecrets}$$

$$s_0 \models \left[\left(\bigsqcup_{1 \leq i, j \leq 6} \neg S_i \Sigma_j?; \text{call}_j^i \right)^5 \right] \neg EK \text{ AllSecrets}$$

Embedding and complexity

Theorem

A planning task $(Act, s_0, goal)$ in normal form is solvable iff

$$s_0 \models \left\langle \left(\bigsqcup_{a \in Act} \text{execAct}(a) \right)^* \right\rangle goal$$

where $\text{execAct}(a)$ encodes action a as a dynamic logic assignment program

(involves storing values of variables to trigger conditional effects correctly)

- proof of correctness of gossip algorithms [in the logic](#)
 - base case and induction step are theorems of the logic

Theorem

Deciding the solvability of an planning task is PSPACE-complete

Encoding into PDDL

- formulas:

$$tr_{PDDL}(S_{i_1} \dots S_{i_m} p) = \begin{cases} (p) & \text{if } m = 0 \\ (\mathbf{S-m} \ i1 \ \dots \ im \ p) & \text{otherwise} \end{cases}$$

$$tr_{PDDL}(\neg\varphi) = (\mathbf{not} \ tr_{PDDL}(\varphi))$$

$$tr_{PDDL}(\varphi_1 \wedge \varphi_2) = (\mathbf{and} \ tr_{PDDL}(\varphi_1) \ tr_{PDDL}(\varphi_2))$$

- conditional effects of actions:

$$\begin{aligned} &(\mathbf{when} \ tr_{PDDL}(cnd(ce)) \\ &(\mathbf{and} \ tr_{PDDL}(\alpha_1) \ \dots \ tr_{PDDL}(\alpha_m) \\ &(\mathbf{not} \ tr_{PDDL}(\beta_1)) \ \dots \ (\mathbf{not} \ tr_{PDDL}(\beta_\ell)))) \end{aligned}$$

- experiments with FDSS-2014

[Röger et al., Int. Planning Competition 2014]

- variants of the gossip problem
 - shared knowledge of order k ; negative goals
- exam problem
 - teacher has prepared exam and keeps printout in his office
 - student's goal: $S_{student} \ ex \wedge \neg S_{teacher} \ S_{student} \ ex$

Conclusion (1)

- knowledge representation with DEL event models:
 - art rather than craft
 - practical problems
 - conceptual problems (type vs. token)
- the other agents' observation should be based on information from the possible worlds model, not from the possible event model
 - edge-conditioned event models [Bolander, 2015]
 - special propositional variable “agent i is watching” [Bolander et al., JoLLI 2016]
 - part of the state, not part of the action!

Conclusion (2)

- a simple epistemic planning problem: gossip
- a simple dynamic epistemic logic based on visibility
 - captures epistemic planning problems
 - in PSPACE (even with common knowledge)
 - can be mapped to classical planning
- related work
 - public actions only
[Kominis&Geffner, ICAPS 2015; 2018]
 - public announcements
[v.Benthem et al., LORI 2015],
[Charrier et al., KR 2016]
 - boolean games [H. et al., IJCAI 2016]
- future work
 - from knowledge to belief?

