# On the delay performance of wireless networks: from hard real-time to delay-tolerant opportunistic networking

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# I am from



Toulouse



### the University of Toulouse (1229)

- Maîtresse de conférence at ENSEEIHT since Sept. 2011 -Engineering school
- 5 teaching departments : Electronics and signal processing. Electrical engineering and control, Computer science and applied maths, Telecommunications and Networking
- Member of the IRIT lab: Research Institute for Computer Science. of Toulouse August 2013

# Where did I go before Toulouse ?

- 2002-2005 ▷ PhD in Computer Science Inria Rhône-Alpes, CITI Iab, University of Lyon / INSA Lyon "Wireless LAN planning"
- 2006-2007  $\triangleright$  **Post-doc**, Stevens Institute of Technology, NJ, USA (working with Cristina Comaniciu)

"Cross-Layer Cooperation for Energy Efficiency in WSNs"

Paul



2007-2010 Description Researcher, Outgoing International Fellowship, European Union FP7 2007-2009 : Stevens Institute of Technology



Lucie

2010 : Inria Rhône-Alpes, CITI lab, University of Lyon / INSA Lyon "Distributed MultiObjective Optimization for Wireless ad hoc nets"

2011-? De Maîtresse de conférences, University of Toulouse, INPT-ENSEEIHT

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# Wireless networking





#### Very wide range of applications now

- Telecommunications (3G, 4G...)
- Wireless Internet access (WiFi, Bluetooth, ...)
- ► Factory automation (WirelessHART, ISA100.11a, ...),
- Sensor networking (802.15.4)
- Wireless social networking,
- Body area networking...

#### All wireless, but... different performance are expected

# Research on performance evaluation of wireless networks

Different metrics may be of interest:

- Capacity, throughput, reliability, ...
- End-to-end communication delays, jitters, ...
- Energy consumption,

During this talk, we will concentrate on the **end-to-end communication delay**, primarily, in the following two case studies:

- Part 1: Real-time wireless networking
- Part 2: Large scale dynamic wireless networking

### Part 1: Real-time wireless networks

#### Wireless is gaining momentum to carry delay-sensitive data

- wireless industrial fieldbuses (WirelessHART, ISA100.11a),
- real-time sensing,
- wireless embedded networks, etc.

For safety-critical applications, **real-time guarantees** have to be provided!



"Rien ne sert de courir ; il faut partir à point"

KJR August 2013 lean de la Fontaine,

# Is wireless compatible with hard real-time?

The main pitfall of wireless communications: its unreliability due to interference, pathloss, fading, collisions, hidden nodes, ...

#### If you embark on a plane



.....you expect all avionics communication flows to arrive on time to the core processing modules, no?

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# Is wireless compatible with hard real-time?

The main pitfall of wireless communications: its unreliability due to interference, pathloss, fading, collisions, hidden nodes, ...

#### If you embark on a plane



.....you expect all avionics communication flows to arrive on time to the core processing modules, no?

Thus, using wireless to send hard real-time avionics data ..... has to be proved to be safe!!!....

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# Why wireless for avionics?

### Gain in weight

In an A380, total cabling weights around 21 tons, which represents 8.5% of the typical empty operating weight of the airplane.

Simplified maintenance and installation



There are 3 redundant networks on board (source: http://www.airliners.net)

Upgrading aircraft

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# Which type of wireless medium access?

A380 network carries  ${\sim}1000$  real-time multicast flows emitted by  ${\sim}100$  core processing modules.

Current 100Mbps switched Ethernet network loaded up to 25%.

#### Time division multiple access

- © Strong real-time guarantees
- © Necessitates a common clock for all end systems
- © May require dedicated hardware

#### Carrier sense multiple access (CSMA/CA)

- © Purely distributed, works well for low loaded networks
- © Off the shelf components widely available
- S May not provide real-time guaranties.

### Calculating a probabilistic bound

Characterize and model the end-to-end delay distribution



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# Bound for a point-to-point communication

### For a point-to-point communication using CSMA/CA

- ► N stationary nodes sharing a common wireless medium
- IEEE802.11 DCF MAC protocol: with or without RTS/CTS mechanism
- ▶ M/M/1 and M/G/1 queue and ideal channel conditions



# Bound for a point-to-point communication

#### Overall analytical distribution derivation

Previous works have addressed this problem (cf. refs in  $[1]^{1}$ )

# Main assumption: **MAC and queueing delays are independent** discrete random variables.

MAC delay is a function of the number of nodes N contending for the medium, not the number of packets in the queue

- Calculate the Probability Generating Function (PGF) (i.e. Z-transform of PMF) for MAC and Queueing delays:  $D_m(Z)$  and  $D_q(Z)$
- Total delay PGF follows  $D_t(Z) = D_m(Z) \times D_q(Z)$
- Invert total delay PGF to retrieve PMF using numerical inversion techniques.

### PGF of total delay

Calculated for M/M/1 and M/G/1 queues, where

- ▶ *E*[*D<sub>m</sub>*] is the mean MAC delay
- $D_m(Z)$  is the PGF of MAC delay

>with M/M/1 queue, the PGF of total delay  $D_t(Z)$ 

$$D_t(Z) = \frac{\frac{1}{E[D_m]} - \lambda}{-lnZ + \frac{1}{E[D_m]} - \lambda}$$

>with M/G/1 queue, the PGF of total delay  $D_t(Z)$  $D_t(Z) = \frac{D_m(Z)(1-Z)(1-\rho)}{1-Z-\lambda(1-D_m(Z))}$ 

where

$$D_m(Z) = (1-p)S(Z) \sum_{x=0}^m \left[ \left( pC(Z) \right)^x \prod_{i=0}^x B_i(Z) \right] + \left( pC(Z) \right)^{m+1} \prod_{i=0}^m B_i(Z)$$

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Mean and PGF of MAC delay are extracted from the well-known Markov chain designed by Bianchi<sup>2</sup> for IEEE802.11 DCF.

MAC delay distribution

$$D_m(Z) = (1-p).S(Z).\sum_{x=0}^m [(p.C(Z))^x \prod_{i=0}^x B_i(Z)] + (p.C(Z))^{m+1}.\prod_{i=0}^m B_i(Z)$$
(1)

Mean MAC delay

$$E[D_m] = D'_m(Z)|_{Z=1}$$
(2)

<sup>&</sup>lt;sup>2</sup>G. Bianchi. Performance analysis of the ieee 802.11 distributed coordination function. Selected Areas in Communications, IEEE Journal on, 18(3):535-547,=2000

### Numerical inversion step

Probability generating function(PGF)

• 
$$D(Z) = \sum_{k=0}^{\infty} d(k) Z^k \xrightarrow{\text{Numerical}} d(k)$$

- Numerical inversion methods:
  - Lattice-Poisson (LP) algorithms[1]
- Two different usage of the LP algorithms
  - The LP inversion formula of Vardakas et all. [9]

$$d(k) \approx \frac{1}{2kr^k} \sum_{j=1}^{2k} (-1)^j Re(D(re^{i\pi j/k}))$$

• The LP inversion formula of Vu et Sakurai [10]

$$d(k) \approx \frac{1}{2klr^k} Re\left(\sum_{j=-kl}^{kl-1} D(re^{-i\pi j/(kl)})e^{i\pi j/l}\right)$$

where  $r = 10^{-\frac{\gamma}{2k}}$ , which results in an accuracy of  $10^{-\gamma}$ 

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# Are all these model accurate?

#### Errors can be introduced by

- MAC or queuing model inaccuracies
- Numerical inversion step.

### Goal of this work

#### Propose a performance evaluation framework to:

- select the best MAC and queuing models
- limit inversion errors

where we **decouple the error** introduced by the model and the numerical inversion.

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# Quantifying the modeling error (1)

Total delay model directly produces the PGF

#### Compare to extensive simulations

#### But without inverting the analytical total delay PFG !

Calculated the PMF  $d^{s}(k)$  from the statistics of the delay obtained by simulation



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### Quantifying the modeling error (2)

Normalized root mean squared error (NRMSE) as

$$f_{model} = \frac{1}{Card(C)} \sum_{Z \in C} \sqrt{\frac{|D^{S}(Z) - D^{a}(Z)|^{2}}{|D^{S}(Z)|^{2}}}$$





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### Quantifying the inversion error (1)

### • A perfect PGF inversion is characterized by $Z\{Z^{-1}\{D(Z), Z\in\mathbb{C}\}\} \equiv \{D(Z), Z\in\mathbb{C}\}$

**Procedure:** 

D

$$a_{m}^{a}(Z) = (1-p)S(Z)\sum_{x=0}^{m} \left[ \left( pC(Z) \right)^{x} \prod_{i=0}^{x} B_{i}(Z) \right] + \left( pC(Z) \right)^{m+1} \prod_{i=0}^{m} B_{i}(Z)$$

$$LP \text{ algorithm}$$

$$Z^{-1} \{ D_{m(Z)}^{a} \}: \ \widehat{d(k)} \approx \frac{1}{2klr^{k}} Re(\sum_{j=-kl}^{kl-1} D_{m}^{a}(re^{\frac{-i\pi j}{kl}})e^{\frac{i\pi j}{l}})$$

$$Z \text{-transform}$$

$$Z \{ Z^{-1} \{ D_{m(Z)}^{a} \} \}: \sum_{k=0}^{\infty} \widehat{d(k)} Z^{k} \qquad O_{m}^{a}(Z)$$

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### Quantifying the inversion error (2)

Normalized root mean squared error (NRMSE) as

$$f_{inv} = \frac{1}{Card(C)} \sum_{Z \in C} \sqrt{\frac{|D(Z) - Z\{Z^{-1}\{D(Z)\}\}|^2}{|D(Z)|^2}}$$

Results



Error bound	Inversion method	$f_{inv}$
$\alpha = 10^{-6}$	Vu and Sakurai	ai 0.0195
$\gamma = 10$	Vardakas et al.	0.0688
$\alpha = 10^{-4}$	Vu and Sakurai	0.0232
$\gamma = 10$	Vardakas et al.	0.1814

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### Results: MAC delay PMF

MAC model is good - Inversion accuracy needs to be controlled



Figure: MAC delay PMF for different accuracies using Vu and Sakurai's LP formula with different accuracies.

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# Results: Queuing delay PMFs

M/G/1 much better for large networks. For small networks, M/M/1 is sufficient!



Figure: Analytical queueing delay PMFs for M/M/1 and M/G/1 queues vs. simulations.

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### Results: Total delay PMFs

#### Total delay is dominated by queuing.



Figure: Analytical total delay PMFs for M/M/1 and M/G/1 queues vs. simulations.

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### Results: Extension to 2-hop communications

#### cf. Paper for details.



Figure: Results for a 2-hop communication of n = 5 nodes, M/M/1 queues.

③Arrival distribution at the relay node is not Poisson (but log-normal)

# Conclusion Part 1:

#### Is wireless compatible with real-time?

- ③ For a point-to-point communication, worst-case probabilistic bounds can be extracted analytically for CSMA/CA.
- © There is performance evaluation framework to test various models and methods that could be used for certification

#### Main challenges

- Extend to multi-hop communications. But will we really need multiple hops in a plane?
- Compare to TDMA solutions with synchronization.

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# Part 2: Large scale dynamic wireless networks

Smartphones have the potential to be:

> visually-aware sonically-aware always-connected directionally-aware location-aware motion-aware



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Creates a dynamic network with high potential for wireless and pervasive applications

- Wireless social networking, global sensing, content distribution,
- ▶ More and more data in transit: 3/4G network offloading...

# Internetworking human beings!

Real-world mobility scenarios create neither purely regular nor purely random connections among the entities composing the network



#### Dynamic Complex Wireless Networks (DCWN)

- Have large number of vertices and edges that exhibit a pattern
- Evolves according to semi-rational decisions of its entities
- Semi-rational decisions:
  - are mostly regular and repeat themselves
  - but may be influenced by random events

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### Data sets

#### Data collection to build contact traces

- Log the contact time and duration of a node to an access point
- Log the GPS coordinates of mobile nodes regularly

Derive a time-varying contact graph

Dataset	Local	#	Duration	Туре	Avg. # encounters/
		entities			node/day
Dartmouth <sup>3</sup>	campus	1156	2 months	Individuals	145.6
USC <sup>4</sup>	campus	4558	2 months	Individuals	23.8
San Francisco <sup>5</sup>	City	551	1 month	Cabs	834.7

- Dartmouth and USC collect connection dates/durations to WiFi APs,
- San Francisco collects GPS locations of taxi cabs.

<sup>3</sup>T. Henderson et al. "The changing usage of a mature campus-wide wireless network," in Proc. of ACM MobiCom 2004

<sup>4</sup> W. jen Hsu et al. "Impact: Investigation of mobile-user patterns across university campuses using wlan trace analysis," CoRR, vol. abs/cs/0508009, 2005

<sup>b</sup>A. Rojas et al. "Experimental validation of the random waypoint mobility model through a real world mobility trace for large geographical areas," in Proc. of the 8th ACM MSWiM 2005

### Rationale and related initiatives

#### Characterize interactions, i.e. edges of contact graph

Regularity of contacts : How often did Arnaud and Paul meet per day? during the whole trace?

Miklas et al.<sup>6</sup> determine whether 2 nodes are *friends* or *strangers* using an empirical threshold (friends encounter 10 times or more within 14 weeks).



<sup>6</sup>A. G. Miklas et al., "Exploiting social interactions in mobile systems," in Proceedings of the UbiComp '07 🗄 🕨 👍 🐑 🔍 🔍

### Rationale and related initiatives

Characterize node's behavior, i.e. vertices of contact graph Using localization information, Zyba et al.<sup>7</sup> differentiate *social* from *vagabond* nodes. Socials appear regularly in a given area while vagabonds visit an area rarely and unpredictably.



Monitor the total appearance and regularity of appearance

Paul is social at the cafeteria but vagabond at the library: a per node/per area approach  $\rightarrow$  geographical dependency

<sup>&</sup>lt;sup>7</sup>G. Zyba, G. Voelker, S. Ioannidis, and C. Diot, "Dissemination in opportunistic mobile ad-hoc networks: The power of the crowd, in *Infocom*'11

### RECAST<sup>8</sup>

- Characterizes the interactions of nodes based on their probability to originate from a random or social behaviour
- Identify different kinds of social interactions (friends, acquaintances, bridges or random)
- ► No geographical dependency, i.e., is of general validity

<sup>&</sup>lt;sup>8</sup> "RECAST: Telling Apart Social and Random Relationships in Dynamic Networks", P. Olmo Vaz de Melo, A. Viana, M. Fiore, K. Jaffrès-Runser, F. Le Moüel and A. A. F. Loureiro, in MSWiM'13.

### Temporal social graphs from contact traces

Two possible representations

1.  $\delta$  event graph:  $\mathcal{G}_k(\mathcal{V}_k, \mathcal{E}_k)$ There is an edge in  $\mathcal{E}_k$  if contact within  $\delta = 1$  day for instance.



#### 2. Accumulative graph $G_t(V_t, E_t)$

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### Temporal social graphs from contact traces

Two possible representations

- 1.  $\delta$  event graph:  $\mathcal{G}_k(\mathcal{V}_k, \mathcal{E}_k)$ There is an edge in  $\mathcal{E}_k$  if contact within  $\delta = 1$  day for instance.
- 2. Accumulative graph  $G_t(V_t, E_t)$ :  $G_t = \{\mathcal{G}_1 \cup \mathcal{G}_2 \cup ... \cup \mathcal{G}_t\}$



 $G_2(V_2, E_2)$  Accumulative graph up to Day 2

Accumulates all event graphs up to time step t.

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# Temporal graphs generation from contact traces

### Example accumulative graph $G_t$ for t = 2 weeks

For  $\delta=1$  day and using force-direct layout algorithm for plotting



Seems difficult to extract any knowledge from these social graphs:  $\rightarrow$  gathers all social AND random interaction!

# Comparing a social graph to its random counterpart

### Random graph equivalent of G

Calculate a random graph  $G^R$  from a graph G(V, E):

- Keep same number of vertices and edges,
- Randomly assign edges to keep the same node degree distribution using RND algorithm<sup>9</sup>:

An edge is set between nodes of degree  $d_i$  and  $d_j$  with probability  $p_{ij} = (d_i \times d_j) / \sum_{k=1}^{|V|} d_k$ 

### Random accumulative graph $G_t^R$

Random accumulative graph derived from event graphs  $\{G_i\}_{i \in [1,..,t]}$ 

$$G_t^R = \{RND(\mathcal{G}_1) \cup RND(\mathcal{G}_2) \cup \ldots \cup RND(\mathcal{G}_t)\}$$

<sup>&</sup>lt;sup>9</sup>F. Chung and L. Lu, "Connected Components in Random Graphs with Given Expected Degree Sequences," Annals of Combinatorics. Nov. 2002

# Comparison social vs. random graphs

Network clustering coefficient can identify a network with an elevated number of clusters (i.e. communities).

If c̄c(G) >> c̄c(G<sup>R</sup>), parts of the decisions of the nodes of G are NOT random



- ▶ Dartmouth / USC traces have an order of magnitude higher  $\bar{cc}$  than  $G^R \rightarrow$  social decisions
- San Francisco: each individual taxi in the trace encounters most of the other taxis → closer to a random behavior

# Social network features: Regularity and Similarity

### Social nodes' behavior tend to

- ▶ repeat on a regular basis (because of daily activities for instance) → Regularity
- ▶ build persistent communities and generate common acquaintances → Similarity

#### Mathematical metrics

Edge persistence per(i, j) <sup>10</sup>:

Percentage of time steps an edge exists over the past discrete time steps in the event graphs  $\{G_i\}_{i \in [1,..,t]}$ 

Topological overlap to(i, j) <sup>11</sup>: Ratio of neighbors shared by two nodes calculated for the accumulative graph G<sub>t</sub>.

 $<sup>^{10}\</sup>text{N.}$  Eagle et al., "From the Cover: Inferring friendship network structure by using mobile phone data," Proceedings of the National Academy of Sciences, Sept. 2009

<sup>&</sup>lt;sup>11</sup>J. P. Onnela et al., "Structure and tie strengths in mobile communication networks", Proc. of the National Academy of Sciences, May 2007  $\langle \Box \rangle + \langle \Box \rangle +$ 

# CCDF of edge persistence per(i, j) after 4 weeks

Individuals tend to see each other regularly



Encounters occur almost in a random fashion



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# CCDF of topological overlap to(i, j) after 4 weeks

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Individuals of  $G_t$  have common neighbors



Common neighbors occur in a random fashion



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### Social vs. random edges

In the random network, we only have a probability of  $10^{-3}$  to have edges with a persistence of more than  $\bar{x}_{per} = 0.17$ .



 $\rightarrow$  Thus, in the social graph  $G_t$ :

• edges with  $per(i,j) > \bar{x}_{per}$  can be classified as *social edges* 

• edges with  $per(i,j) < \bar{x}_{per}$  can be classified as *random edges* Note that there is a  $p_{rnd}$  chance that a social edge is actually random (mis-classification)

# **RECAST** classification algorithm

Only parameter of RECAST:  $p_{rnd}$ , the mis-classification error bound. Main steps

- Calculate the per(i,j) and to(i,j) for each edge
- Knowing  $p_{rnd}$ , calculate  $\bar{x}_{per}$  and  $\bar{x}_{to}$  from CCDF's
- For each edge,
  - If per(i,j) > x̄<sub>per</sub> → (i,j) is social for edge persistence else (i,j) is random for edge persistence
  - if to(i,j) > x̄<sub>to</sub> → (i,j) is social for topological overlap else (i,j) is random for topological overlap
- Classify edges into classes of relationships according to:

Class	Edge persistence	Topological overlap
Friends	social	social
Acquaintances	random	social
Bridges	social	random
Random	random	random
	•	

# Snapshots after 2 weeks



Friends edges are in blue, Bridges edges are in red Acquaintance edges are in gray, Random edges are in orange

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# Cluster coefficient analysis for only random edges



Validates the efficiency of RECAST to identify random edges for Dartmouth and USC

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### Classification results after 4 weeks

Number of edges of a each class that appear in the first 4 weeks vs.  $p_{rnd}$ 



RECAST is not sensitive to  $p_{rnd}$  !

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# Epidemic data dissemination results

#### Is it worth accounting for the social edges?

- Let's assume we start an epidemic transmission between a source and a destination that share a edge in the social network. (Social graph calculated with 4 first weeks of data set)
- Which edges participate in the forwarding in the following 2 weeks?



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# Epidemic data dissemination: Path length

#### Is it worth accounting for the social edges?

- For both data sets, a majority of routes to social edges have a path length ≤ 3, while only a few percents of routes to random edges do.
- The transfer is much faster between nodes that share a social relationship.
- Edge persistence has a strong impact on the routing efficiency
- But random edges help as well...



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# Conclusions and future works

### RECAST

- requires a unique parameter
- combines user encounter frequency with their 2-hop social network ties
- identifies different kinds of social interactions: friendship, acquaintanceship and bridges

Different mobility traces may have completely different behaviors (San Francisco vs. USC)

#### Future works

- Provide a distributed RECAST classification
- Assess RECAST using data sets with ground truth
- Study spatio-temporal correlations of data sets

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### Thank you for your attention

First beta-version of RECAST classifier available on :
http://www.irit.fr/~Katia.Jaffres/RECAST/Recast-code.zip



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