



# A Stepwise Refinement based Development of Self-Organizing Multi-Agent Systems: Application on the Foraging Ants

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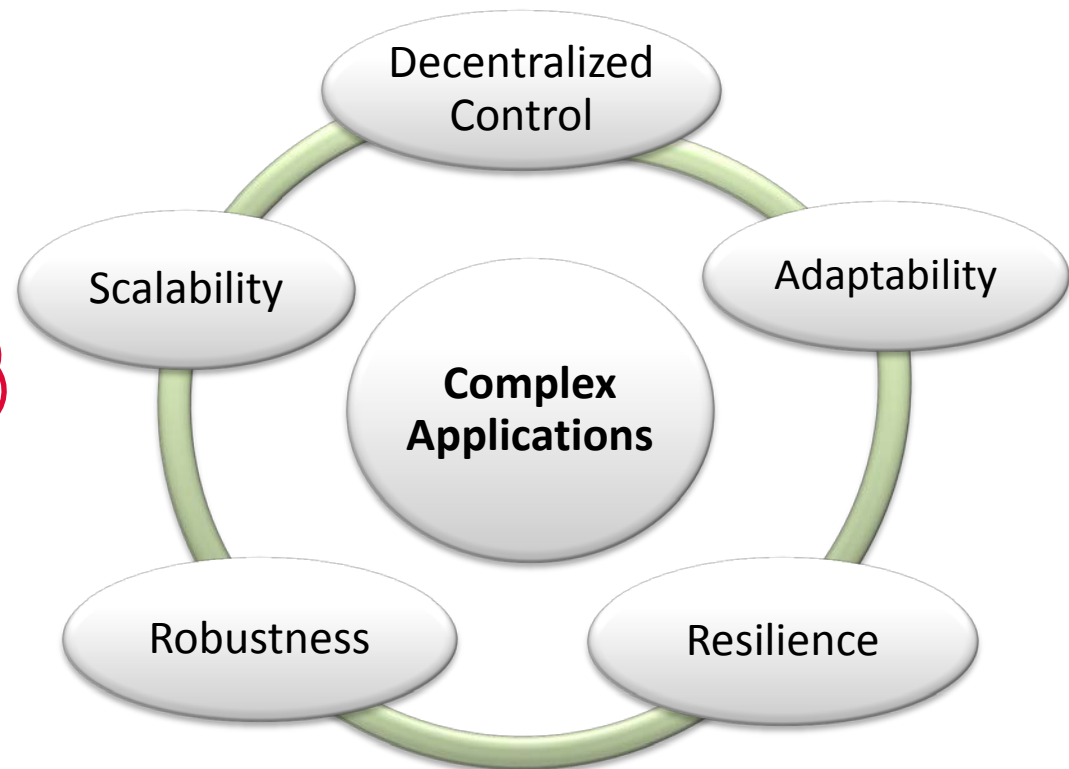
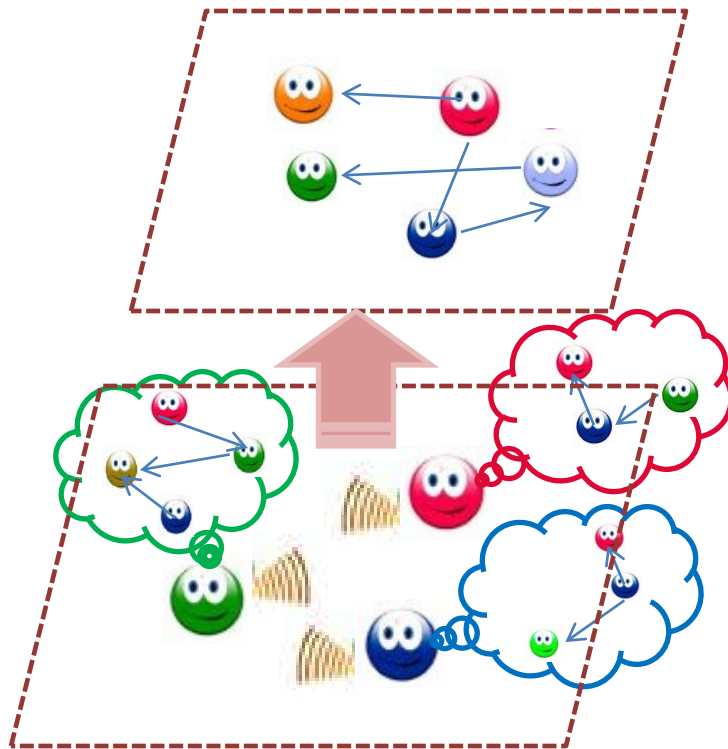
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# Talk outline

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- Context & Motivations
- Formal Development of SO-MAS
- Case Study: Foraging Ants
- Perspectives

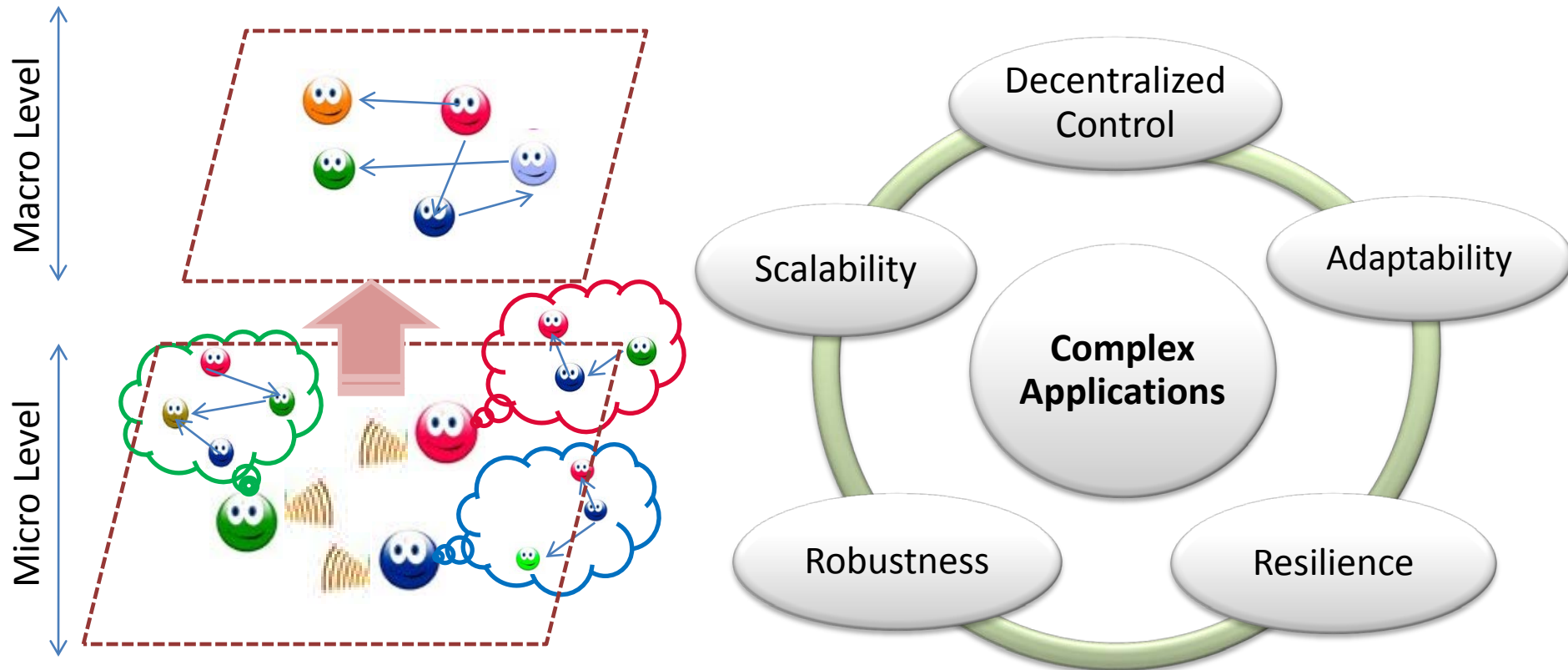
# Context & Motivations



What guarantees related to robustness and resilience can be given?

- ➔ Need for rigorous approaches
- ➔ Our proposition: an approach based on formal techniques.

# Our Approach in a Nutshell



What guarantees related to robustness and resilience can be given?

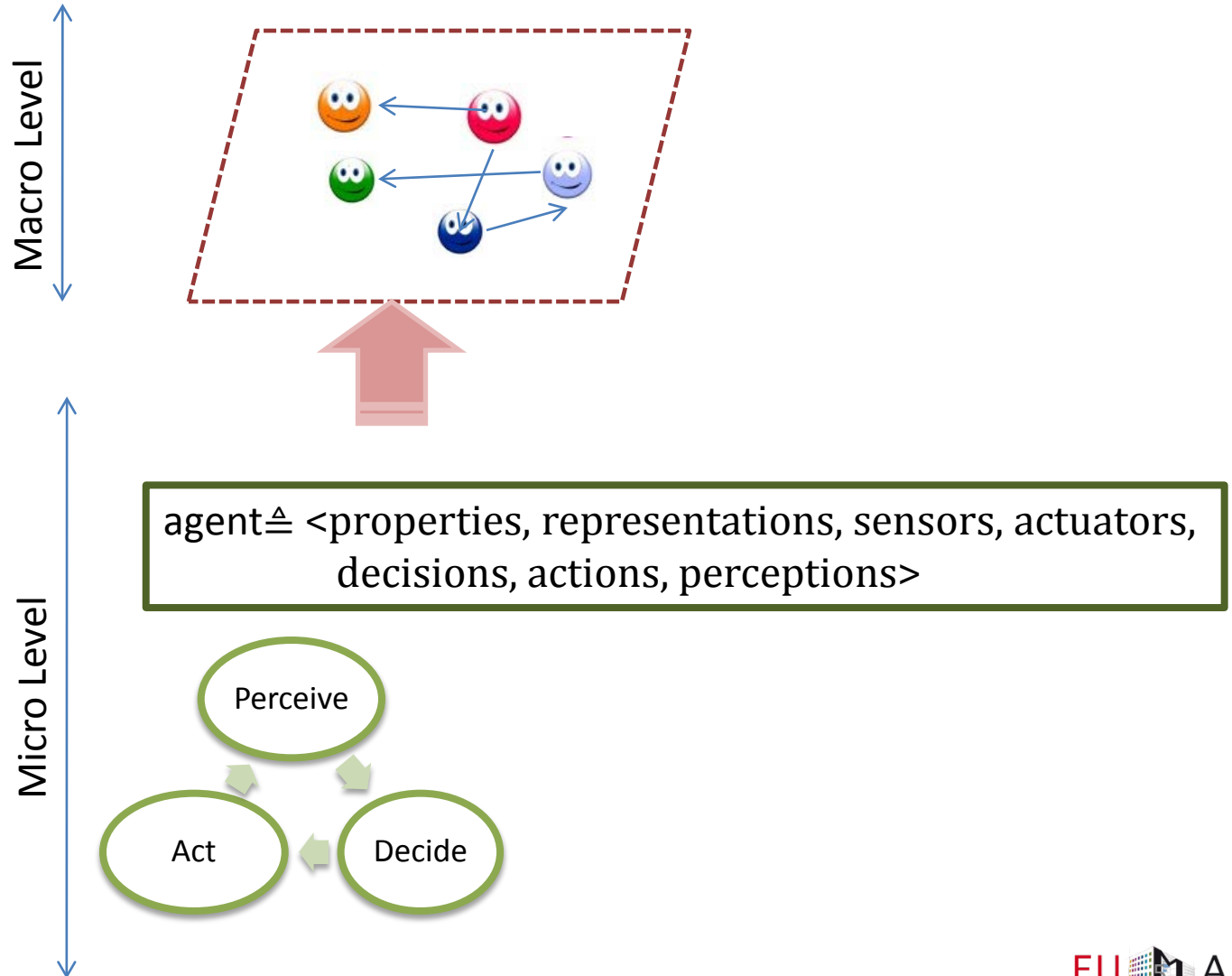
➔ Need for rigorous approaches allowing a systematic verification.

➔ Our proposition: an approach based on formal techniques.

# Our Approach in a Nutshell

The approach  
relies on:

- 1 Two levels of  
observation:  
Micro & Macro



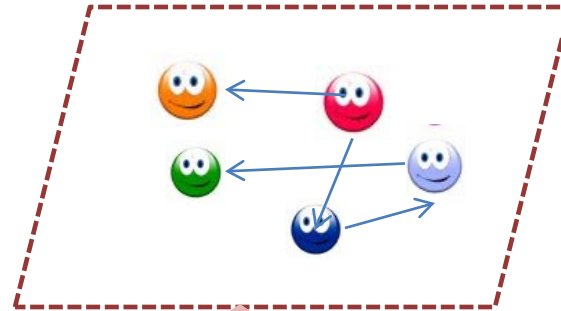
# Our Approach in a Nutshell

The approach relies on:

① Two levels of observation:  
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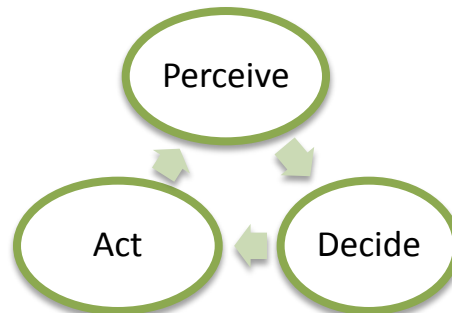
② Stepwise refinement steps  
Event-B

Macro Level



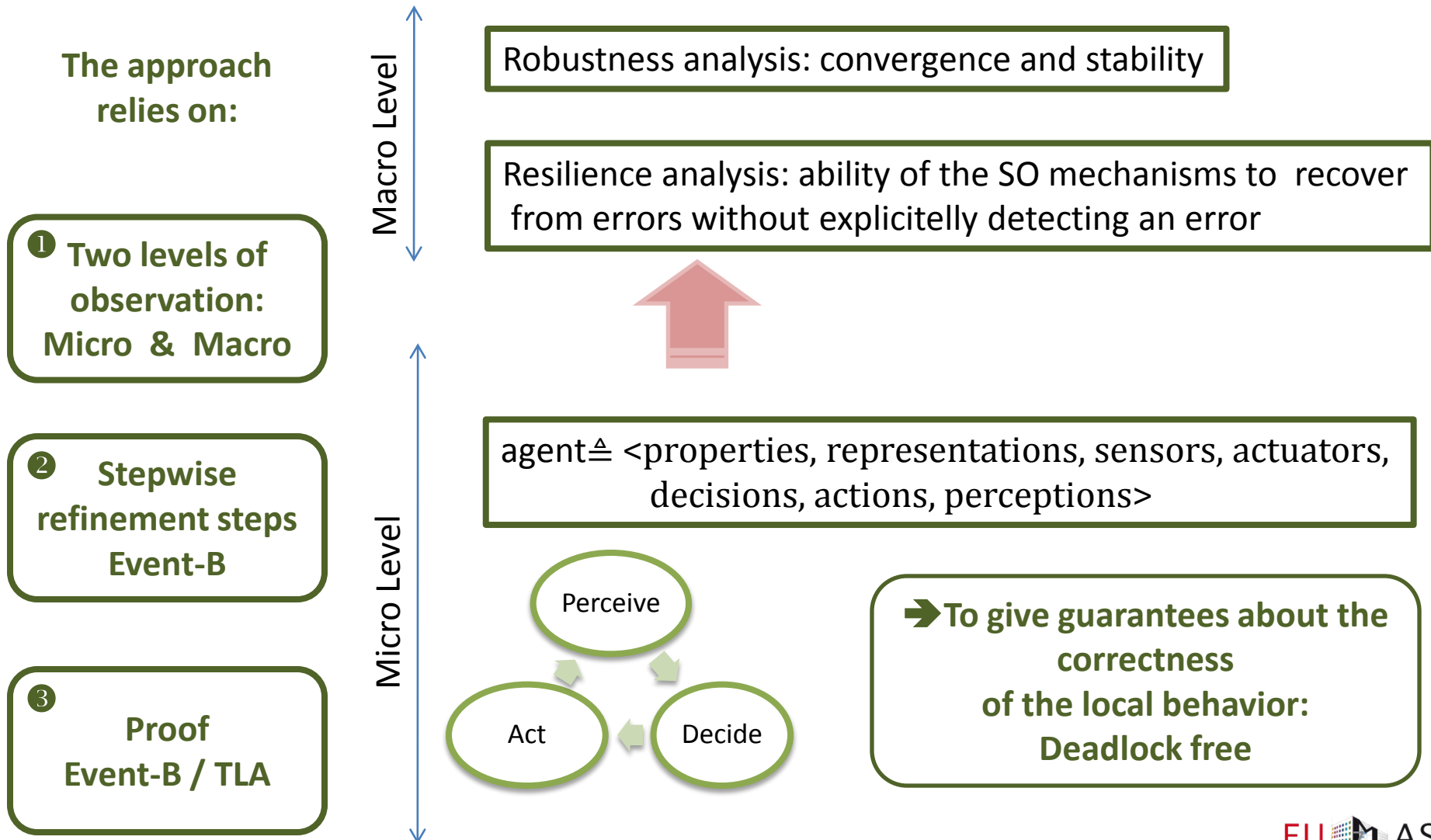
Micro Level

agent  $\triangleq$  <properties, representations, sensors, actuators, decisions, actions, perceptions>



➔ To give guarantees about the correctness of the local behavior:  
Deadlock free

# Our Approach in a Nutshell



# Foraging ants case Study: Description

## ❑ Micro Level

- ❑ Every ant is an agent
- ❑ Properties : current location
- ❑ Representations: food, pheromone, obstacles and ants
- ❑ Decision: choose the next location
- ❑ Actions: Move, Drop pheromone, Harvest food, Drop food
- ❑ Local properties
  - ❑ LocProp1: the ant functions according to the perceive-decide-act cycle
  - ❑ LocProp2, LocProp3: Deadlock freeness respectively in decide and act step of the ant life cycle
  - ❑ LocInv1: the ant should avoid obstacles.
  - ❑ LocInv2: a given location can not contain both obstacle and food.



## ❑ Macro level

- ❑ C1. The ants are able to reach any source of food.
- ❑ C2. The ants are able to bring all the food to the nest
- ❑ S1. When a source of food is reached, the ants are able to focus on its exploitation
- ❑ R1. The ants focusing on exploiting a source of food, are able to continue their foraging activity when this source of food suddenly disappears



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# Event-B and Rodin

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## □ Event-B

- A formal language for systems modelling and analysis based on set theory and first order logic .
- Key feature: use of refinement to represent the system at different level of abstraction
- An Event-B model can be
  - Context: static part
  - Machine: dynamic part

## □ Rodin tool

- Gives an effective support for refinement and mathematical proof
  - Generating Proof Obligations
  - Offering an interactive environment for doing proof

# Our Approach Applied to the Ants

## Ants0 Machine

Three events:

- Perceive
- Decide
- Act

One variable:

- stepAgent
- ➔ LocProp1

First Refinement

## Ants1 Machine

① Refining the Act event

② Introducing QuFood  
and Obstacles

➔ Locinv1

➔ LocInv2

➔ LocProp2: Deadlock  
freeness in the Act

Second Refinement

## Ants2 Machine

① Refining the Decide  
event

② Introducing the  
actuators and the  
nextLocation

③ Refining the Act  
▪ witnesses

Third Refinement

## Ants3 Machine

① Refining the Perceive event

② Introducing the sensors and  
the representations

③ Introducing pheromone  
distribution

④ Refining the Act events

⑤ Refining the Decide Events

➔ LocProp3: Deadlock freeness  
in the Decide step

Micro Level Modelling

# Global Properties Modelling – Stability

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- ❑ Purpose: to prove the stability property
  - ❑ S1. When a source of food is reached in a particular location *loc1*, the ants are able to focus on its exploitation.
  - ❑  $QuFood(loc1)$  will decrease
- ❑ More formally:
  - ❑  $P \triangleq Inv \wedge QuFood(loc1)=n+1$
  - ❑  $Q_{Harvest} \triangleq Inv \wedge QuFood(loc1)=n$
  - ❑  $P \rightsquigarrow Q_{Harvest} \triangleq \Box(P \Rightarrow \Diamond Q_{Harvest})$

# Global Properties Modelling – Stability (cont.)

$$\text{SF1.1} \quad P \wedge [N]_{QuFood(loc1)} \Rightarrow (P' \vee Q'_{Harvest})$$

$$\text{SF1.2} \quad P \wedge \langle N \wedge A_{Harvest} \rangle_{QuFood(loc1)} \Rightarrow Q'_{Harvest}$$

$$\text{SF1.3} \quad \Box P \wedge \Box [N]_{QuFood(loc1)} \Rightarrow \Diamond Enabled \langle A_{Harvest} \rangle_{QuFood(loc1)}$$

$$\text{SF1.H} \quad \Box [N]_{QuFood(loc1)} \wedge SF_{QuFood(loc1)}(A_{harvest}) \Rightarrow P \rightsquigarrow Q_{Harvest}$$

- $N \triangleq \text{Act\_Mov\_Random} \vee \text{Act\_Mov\_Foll\_Food} \vee \text{Act\_Mov\_Foll\_Phero} \vee \text{Act\_Harv\_Food}$
- $A_{Harvest} \triangleq \text{Act\_Harv\_Food}$
- SF1.1: progress step, either  $P$  or  $Q_{Harvest}$  can be reached.
- SF1.2: inductive step,  $Q_{Harvest}$  is reached.
- SF1.3:  $\langle A_{Harvest} \rangle_{QuFood(loc1)}$  will be eventually enabled
- $SF_{QuFood(loc1)}(A_{Harvest}) \triangleq \Box \Diamond Enabled \langle A_{Harvest} \rangle_{QuFood(loc1)} \Rightarrow \Box \Diamond \langle A_{Harvest} \rangle_{QuFood(loc1)}$

# Global Properties Modelling – Stability (cont.)

➔ Assumption: Once an ant smells food on *loc1*, other ants will be able also to smell this food and follow it .

$$WF_{QuFood(loc1)}(A_{FollowFood}) \triangleq \Diamond \Box Enabled \langle A_{FollowFood} \rangle_{QuFood(loc1)} \Rightarrow \Box \Diamond \langle A_{FollowFood} \rangle_{QuFood(loc1)}$$

$$\square \quad SF1.3 \triangleq \Box P \wedge \Box [N]_{QuFood(loc1)} \Rightarrow \Diamond Enabled \langle A_{Harvest} \rangle_{QuFood(loc1)}$$

$\square$  Purpose: to prove

$$SF1.31 \triangleq \Box [N]_{QuFood(loc1)} \Rightarrow P \rightsquigarrow \Diamond Enabled \langle A_{Harvest} \rangle_{QuFood(loc1)}$$

$$Q_{FollowFood} \triangleq Enabled \langle A_{Harvest} \rangle_{QuFood(loc1)}$$

$$A_{FollowFood} \triangleq Act\_Follow\_Food$$

$$WF1.311 \quad P \wedge [N]_{QuFood(loc1)} \Rightarrow (P' \vee Q'_{FollowFood})$$

$$WF1.312 \quad P \wedge \langle N \wedge A_{FollowFood} \rangle_{QuFood(loc1)} \Rightarrow Q'_{FollowFood}$$

$$WF1.313 \quad P \Rightarrow Enabled \langle A_{FollowFood} \rangle_{QuFood(loc1)}$$

$$WF1.31 \quad \Box [N]_{QuFood(loc1)} \wedge WF_{QuFood(loc1)}(A_{FollowFood}) \Rightarrow P \rightsquigarrow Q_{FollowFood}$$

# Perspectives

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- ❑ Global properties proof under Rodin tool
- ❑ Reasoning about the convergence and resilience global properties.
- ❑ Generalizing the approach by defining design patterns in order to automate the formal development.
- ❑ Integration of the proposed formal framework within a SO-MAS development method.

Thank You!  
Questions & Feedback  
are Welcome